

Segmentation Using Superpixels: A Bipartite Graph Partitioning Approach

Zhenguo Li Xiao-Ming Wu Shih-Fu Chang
Columbia University

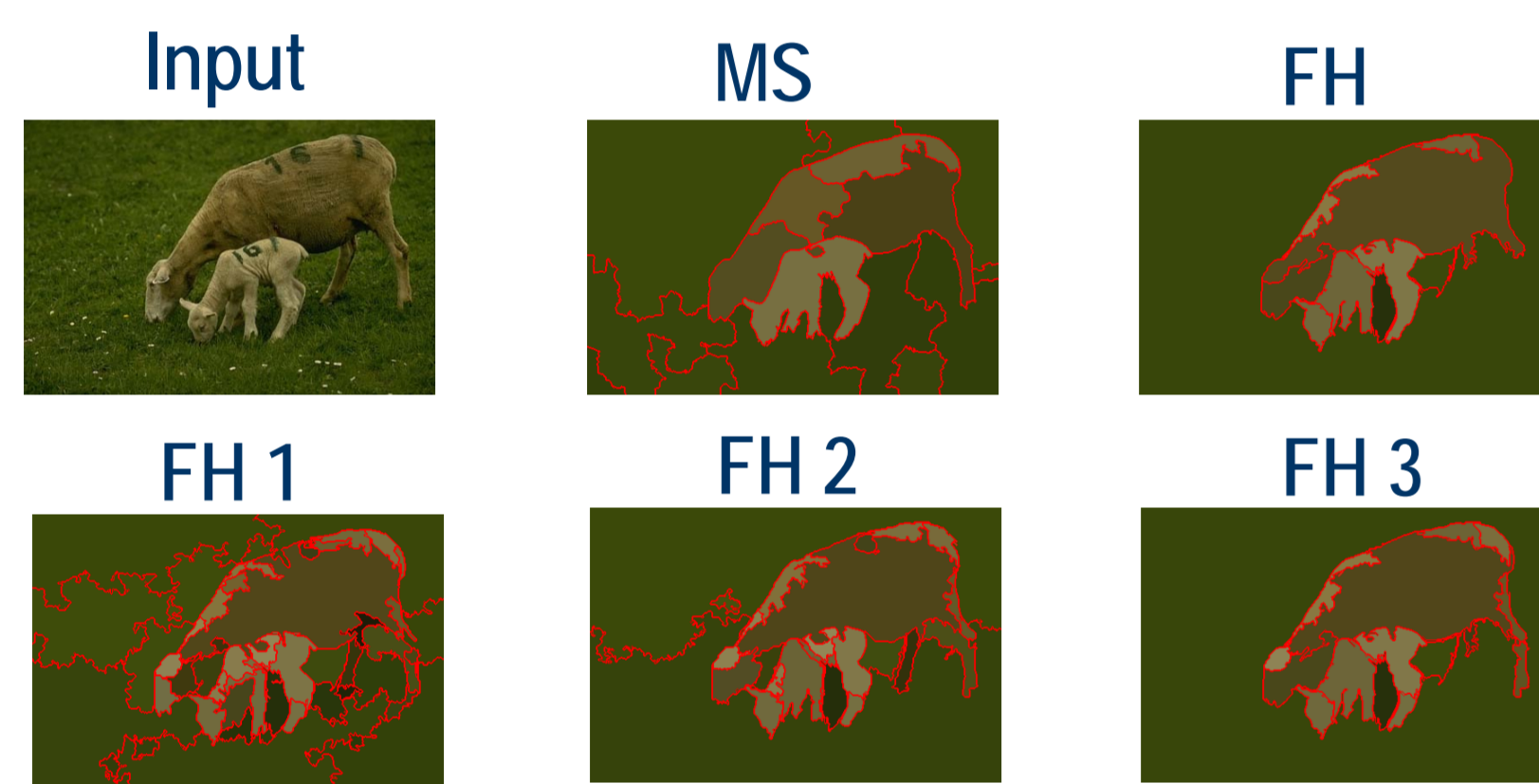


Problem and Motivations

Segmentation is crucial for high-level vision. It remains challenging due to visual ambiguity and variety.

Observations

- Different methods behave differently.
- Each method gives different results under different parameters.

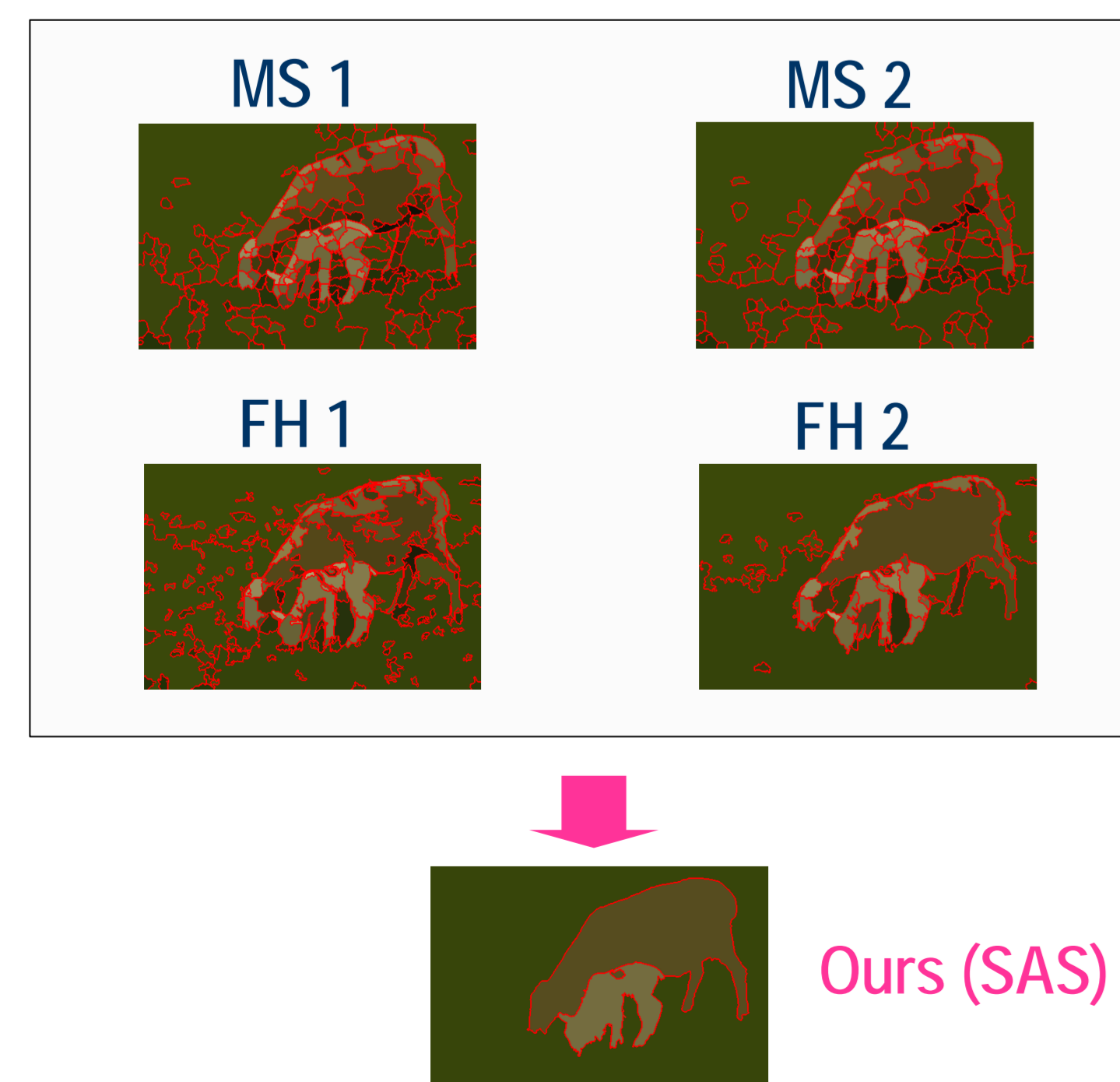


MS [Comaniciu and Meer'02]
FH [Felzenszwalb and Huttenlocher'04]

How to capture and model a variety of visual patterns simultaneously?

Motivations

- Combine complementary information to improve performance.
- Capture visual patterns using superpixels generated by different methods with varying parameters.



Superpixel Aggregation and Bipartite Graph Partitioning

- Combine pixels and multiple/multi-scale segmentations by a bipartite structure. Using superpixels as grouping cues:
 - Pixels in a superpixel tend to belong together.
 - Similar neighboring superpixels tend to belong together.

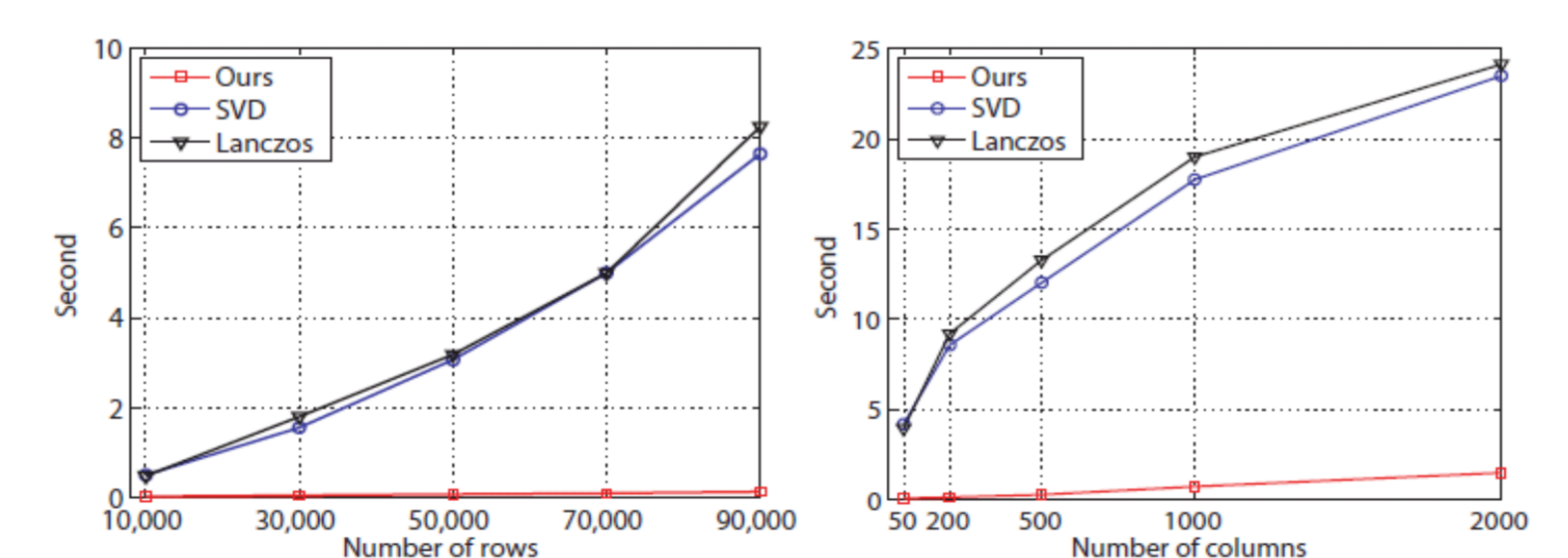
Algorithm 1 Transfer Cuts

Input: A bipartite graph $G = \{X, Y, B\}$ and a number k .
Output: A k -way partition of G .

- Form $D_X = \text{diag}(B1)$, $D_Y = \text{diag}(B^T 1)$, $W_Y = B^T D_X^{-1} B$, and $L_Y = D_Y - W_Y$.
- Compute the bottom k eigenpairs $\{(\lambda_i, v_i)\}_{i=1}^k$ of $L_Y v = \lambda D_Y v$.
- Obtain γ_i such that $0 \leq \gamma_i < 1$ and $\gamma_i(2 - \gamma_i) = \lambda_i$, $i = 1, \dots, k$.
- Compute $f_i = (u_i^T, v_i^T)^T$, with $u_i = \frac{1}{1-\gamma_i} D_X^{-1} B v_i$, $i = 1, \dots, k$.
- Derive k groups of $X \cup Y$ from f_1, \dots, f_k .

Speedup by the bipartite structure

Algorithm	Complexity
Lanczos [26]	$O(k(N_X + N_Y)^{3/2})$
SVD [31]	$O(k(N_X + N_Y)^{3/2})$
Ours	$2k(1 + d_X)N_X \text{ operations} + O(kN_Y^{3/2})$

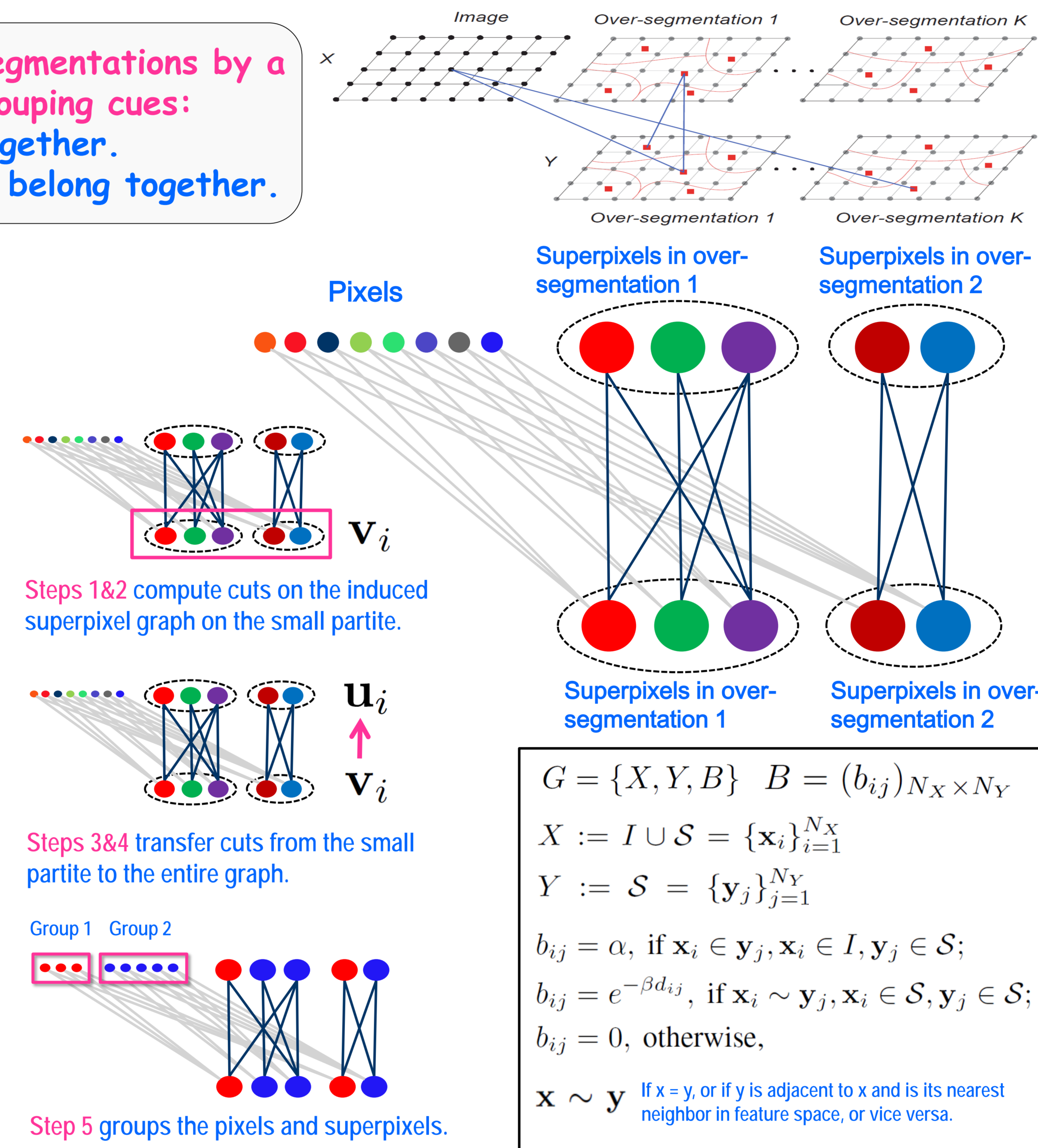


Algorithm 2 Segmentation by Aggregating Superpixels

Input: An image I and the number of segments k .
Output: A k -way segmentation of I .

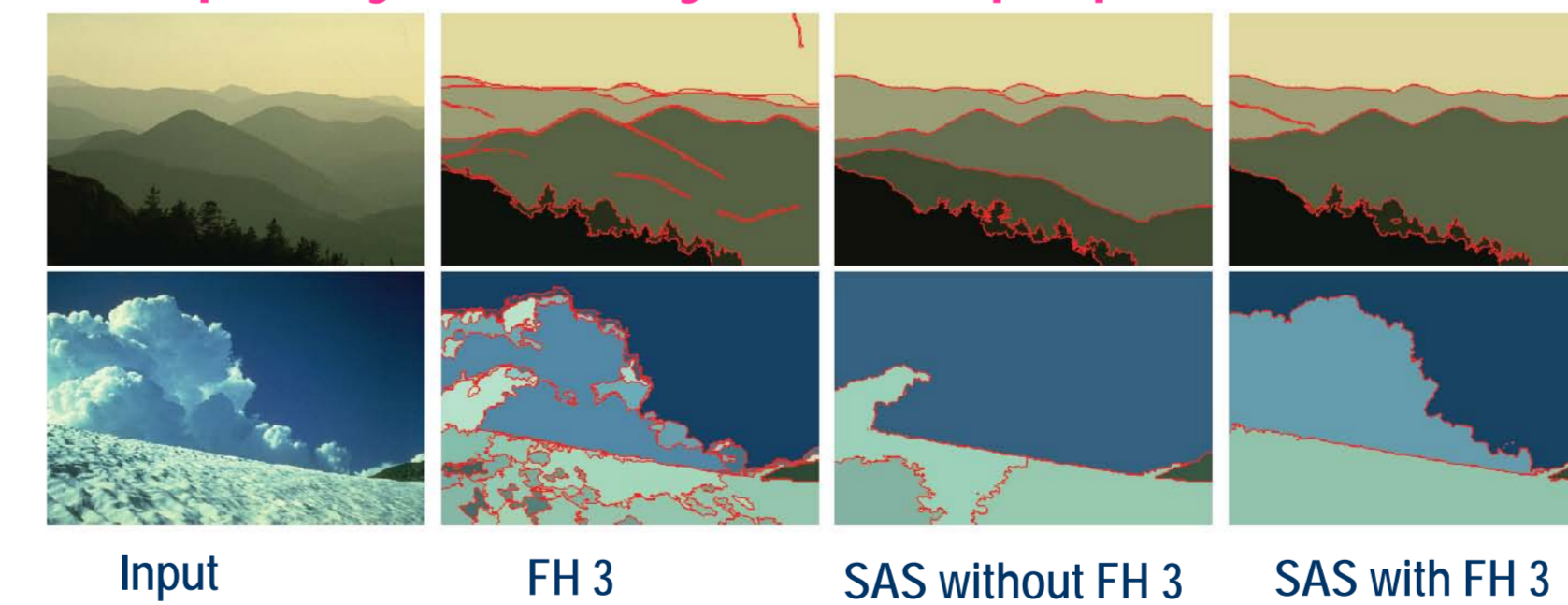
- Collect a bag of superpixels \mathcal{S} for I .
- Construct a bipartite graph $G = \{X, Y, B\}$ with $X = I \cup \mathcal{S}$, $Y = \mathcal{S}$, and B defined in (1-3).
- Apply Tcut in Algorithm 1 to derive k groups of G .
- Treat pixels from the same group as a segment.

SAS takes 6.44s per image of size 481×321 , where 4.11s for generating superpixels and 0.65s for Tcut. MNcut, MLSS, and TBES take more than 30s, 40s, 150s, and 500s, respectively. Codes of SAS are available at: www.ee.columbia.edu/dvmm.



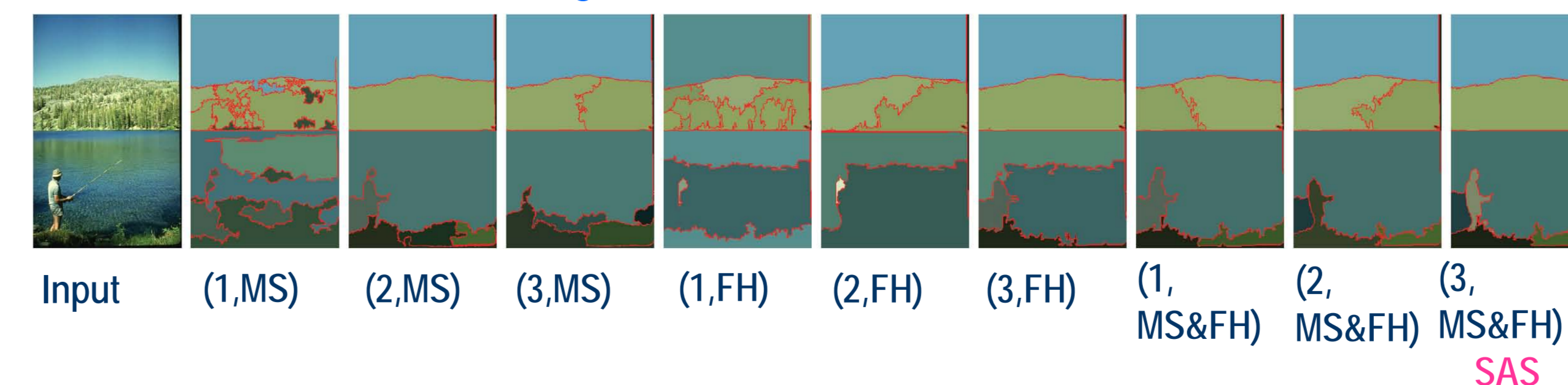
Include large superpixels for complex images to suppress strong edges within objects.

Adaptively select layers of superpixels.



Segmentations with different combinations of layers of superpixels.

(3, MS&FH): use three over-segmentations from each method.



Segmentation Results

Results on Berkeley segmentation database (BSDS)

Methods	PRI	VoI	GCE	BDE
Ncut	0.7242	2.9061	0.2232	17.15
Mean Shift	0.7958	1.9725	0.1888	14.41
FH	0.7139	3.3949	0.1746	16.67
JSEG	0.7756	2.3217	0.1989	14.40
MNcut	0.7559	2.4701	0.1925	15.10
NTP	0.7521	2.4954	0.2373	16.30
SDTV	0.7758	1.8165	0.1768	16.24
TBES	0.80	1.76	N/A	N/A
UCM	0.81	1.68	N/A	N/A
MLSS	0.8146	1.8545	0.1809	12.21
SAS	0.8319	1.6849	0.1779	11.29
SAS(MS)	0.7991	1.9320	0.2222	15.37
SAS(FH1)	0.8070	1.8690	0.2167	14.28
SAS(FH2)	0.8007	1.7998	0.2105	17.17
SAS(MS+FH1)	0.8266	1.7396	0.1868	11.83
SAS(MS+FH2)	0.8246	1.7144	0.1904	12.63

Methods	FH	Ncut	Mean Shift	UCM	SAS
BFM	0.58	0.62	0.63	0.71	0.64
RSC	0.51	0.44	0.54	0.58	0.62

PRI: Probabilistic Rand Index; VoI: Variation of Information; GCE: Global Consistency Error; BDE: Boundary Displacement Error; BFM: Boundary-based F measure; RSC: Region-wise segmentation covering.

Sensitivity of SAS w.r.t. the parameters.

α	$\{10^{-9}, 10^{-5}, 10^{-1}, 10^3\}$				10^{-3}			
β	20				$2 \times \{10^{-5}, 10^{-1}, 10^3, 10^7\}$			
PRI	0.806	0.813	0.818	0.818	0.821	0.821	0.814	0.815
VoI	1.867	1.810	1.836	1.840	1.811	1.811	1.836	1.831
GCE	0.209	0.203	0.201	0.202	0.194	0.194	0.210	0.209
BDE	13.76	13.33	13.27	13.31	12.40	12.35	13.70	13.70

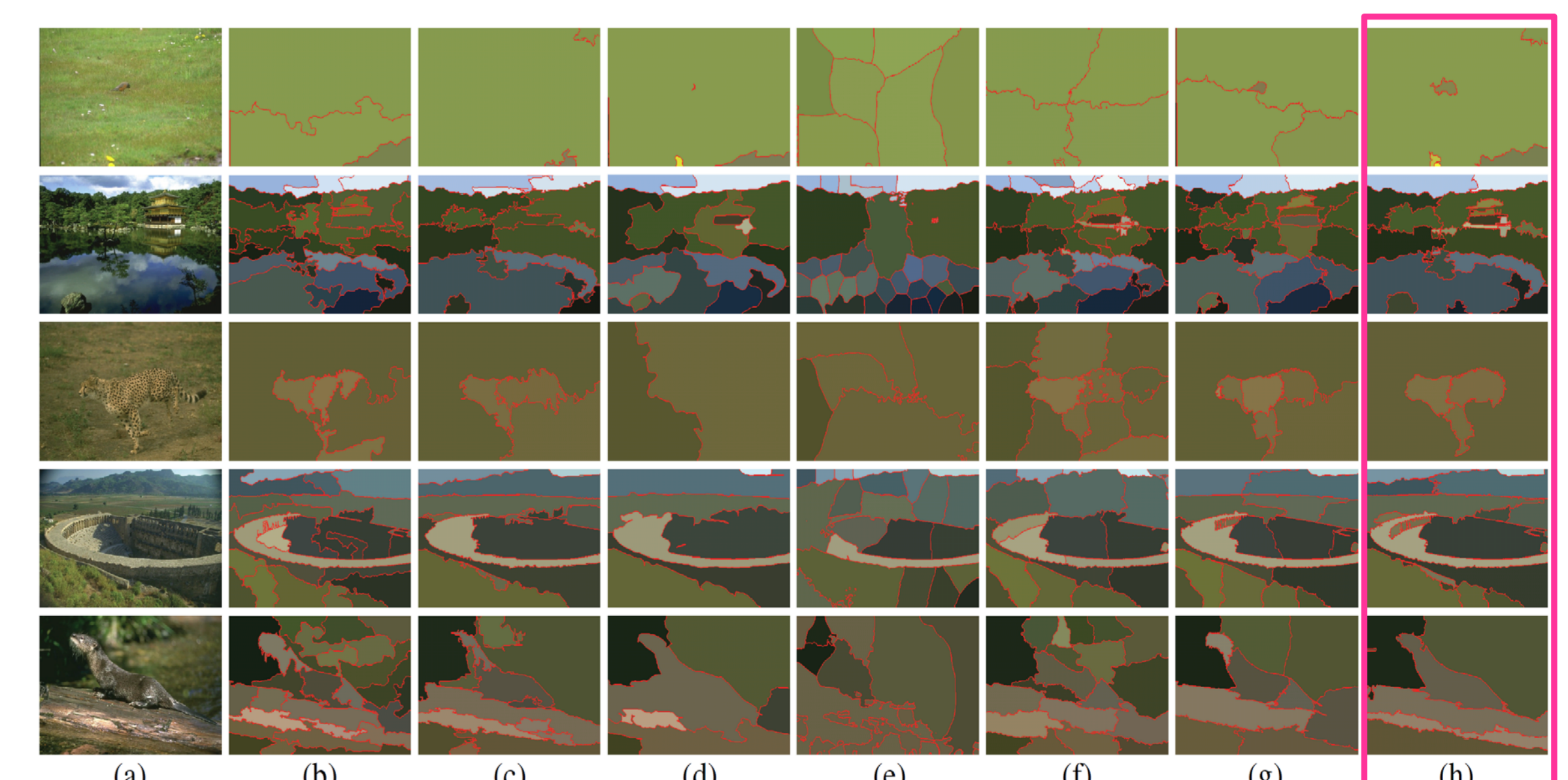


Figure 5. Segmentation examples on Berkeley Segmentation Database. (a) Input images. (b) Mean Shift. (c) FH. (d) TBES. (e) Ncut. (f) MNcut. (g) MLSS. (h) SAS.