SLAW: Secure Localization Against Wormhole Attacks Using Conflicting Sets

Honglong Chen*, Wei Lou*, and Zhi Wang†

*Department of Computing, The Hong Kong Polytechnic University, Kowloon, Hong Kong
†State Key Laboratory of Industrial Control Technology, Zhejiang University, Hangzhou, China

Email: {cshlchen, csweilou}@comp.polyu.edu.hk, wangzhi@iipc.zju.edu.cn

Abstract—The wormhole attack is a severe attack that can be easily mounted on a wide range of wireless networks without compromising any cryptographic quantity or network node. In the wormhole attack, an attacker sniffs packets at one point in the network, tunnels the packets through a wired or wireless link to another point. Such kind of attack can cause severe problems in wireless sensor networks, especially deteriorate the routing process and the localization process. In this paper, we propose a secure localization scheme against wormhole attacks, which includes three phases: wormhole attack detection, neighboring locators differentiation and secure localization. The main idea of the proposed secure localization scheme is to build a so-called conflicting set for each locator according to the abnormalities of message exchanges among neighboring locators, which is used to differentiate the dubious locators from valid locators for the secure localization. The simulation results show that the proposed scheme outperforms the existed schemes under different network parameters.

Keywords: Secure Localization; Wormhole Attacks; Wireless Sensor Networks.

I. INTRODUCTION

In most wireless sensor network (WSN) applications, such as emergency response systems, military field operations, and environment monitoring systems, the inanition of measurement data without location information makes the self-localization capability a highly desirable characteristic of the systems. Most localization algorithms for WSNs estimate the positions of location-unknown nodes based the position information of a set of nodes (locators) and the inter-node measurements. The localization techniques can be classified into range-based and range-free schemes. Range-based localization assumes that the distances between sensors and locators can be estimated by using different measurements, such as the arrival time (ToA [1]), the time difference of arrival times (TDoA [2]), the arrival angel (AoA [3]), or the received signal strength indicator (RSSI [4]), etc. Range-free localization relies on other features of the network, such as hop counts [3], centroid [5], APIT [6], amorphous computation [7], directional antenna [8], signal fingerprinting [9], etc.

Despite the recent advances of localization in WSNs [10], most of the existing localization systems are vulnerable under the adversarial scenario where malicious attacks can disturb the localization process. For example, a simple replay attack may defunct the distance measurement, leading to the malfunction of the range-based localization technique. Therefore, security is a significant characteristic of the localization process in the hostile environment.

The attackers, which threaten the localization of the sensor nodes in a hostile WSN, can generally be classified into two categories, external attackers and internal attackers [11]. External attackers can distort network behaviors without the system’s authorization, while internal attackers are authenticated ones and thus more devastating to the security of the system. The wormhole attack, which is a severe attack, can be easily launched by two colluding external attackers. Khabbazian et al. [12] address how the wormhole attack impacts on the routing protocols when building the shortest paths. In this paper, we will further analyze the impacts of the wormhole attacks on the localization procedures in WSNs.

In our early work [13] [14], secure localization schemes are proposed to defend against wormhole attacks under a simplified system model where all types of nodes have the identical transmission range, the nodes can receive all the transmissions without any message collisions, and attackers will relay all received packets without any message drop-offs. Under such system model, the sensor can easily detect the existence of the wormhole attack and provide dependance against the attack during localization process. However, these schemes do not work well when a general system model is considered where the transmission ranges of different types of nodes are different, the nodes may miss certain packets due to message collisions, and attackers may randomly drop off packets they overhear. In this paper, therefore, we consider the localization problem under this general system model and propose a Secure Localization scheme Against Wormhole attacks called SLAW, which works well under this system model. The SLAW consists of three phases: wormhole attack detection, neighboring locators differentiation and secure localization. The main idea of the SLAW is to make use of the properties of the network to detect the existence of the wormhole attack and to build a so-called conflicting set for each locator so as to identify the dubious locators for the secure localization process.

The main contributions of this paper are summarized as follows:

- We propose a wormhole attack detection approach which can detect the existence of a wormhole attack when the localization process of a sensor node is under the
We propose to use the conflicting set of each locator to differentiate sensor’s neighboring locators. Two independent algorithms are proposed to work for different wormhole attacks:

- We propose a novel secure localization scheme which is divided into three phases: wormhole attack detection, neighboring locators differentiation and secure localization;
- We conduct simulations to demonstrate the effectiveness of the proposed scheme with a general system model under different network parameters.

The remainder of this paper is organized as follows. In Section II, the related work on secure localization is discussed. Section III gives the problem statement. Section IV describes SLAW in details and Section V presents the performance evaluation. Section VI concludes this paper and outlines our future work.

II. RELATED WORK

The security of localization has been well studied in the past few years. The approaches of providing secure localization for WSNs in hostile environments are summarized in [15]. Most of these solutions achieve security by using cryptography (such as the global preloaded key in ROPE [16], the network-wide group key in DRBTS [17], the message authentication in [18]), detecting nodes’ misbehavior (such as malicious beacon signals in [19], time-bounded nonces in [20], position validity in [21]), verifying location information (such as the verifiable multilateration in SPINE [11], the distance verification in ROPE [16], group-based deployment model in LAD [22]), filtering out erroneous and outlier data (attack-resistant MMSE [23], cluster-based MMSE [24]), making statistical decision (such as voting-based scheme in [23], reputation-based scheme in DRBTS [17], robust statistical method in [25]), etc. As all these approaches are application dependent, their performance is affected by the types of attacks and the allocated resources.

As wormhole attacks are launched with external attackers which do not need to compromise any system cryptography, they cannot be defeated by using cryptographic solutions. Thus, the researchers have proposed some wormhole attack detection approaches: The “packet leashes” mechanism [26] uses geographical and temporal leashes to detect whether or not the packets are attacked by wormhole attacks. A similar approach is proposed in [27] based on end-to-end location information rather than hop-by-hop geographical leashes. Another set of wormhole prevent techniques [28]–[30] use the round-trip time of packets as a measurement to determine the existence of wormhole attacks, which are similar in nature to temporal packet leashes. EDWA [31] and WODEM [32] use end-to-end hop counts to detect the wormhole attack and pinpoint location of the attackers. [33] also uses a hop counting procedure to reconstruct local maps for each node and uses a “diameter” feature to detect abnormalities caused by wormholes. LiteWorp [34] takes advantage of two-hop neighbor information of the stationary network to reject the packets brought by wormhole attacks. MobiWorp [35] uses a secure central authority to isolate the malicious node globally when it detects the wormhole. [36] uses directional antennae to obtain relative direction information to verify possible neighbors. Wang et al. [37] [38] propose to detect wormholes by visualizing the entire network topology with some anomalies introduced by attacks. [39] uses the network connectivity information to detect wormhole attacks based on the fact that the independent neighbors of two non-neighboring nodes are upper-bounded. A topological approach is proposed in [40] to detect the wormhole attacks. In [41], a localized algorithm that detects the wormhole attacks directly using the connectivity information implied by the underlying communication graph is designed, and it requires no specialized hardware, which makes it practical in the real-world scenarios. However, all the above wormhole detection schemes emphasize the detection without considering the localization scenario.

The directional antennae are used in the SeRLoc [8] to detect the wormhole attack based on the sector uniqueness property and communication range violation property, and the secure localization can be achieved after identifying the attacked locators. HiRLoc [42] further improves the SeRLoc by utilizing antenna rotations and multiple transmit power levels, which provide more information to increase the localization accuracy. The schemes in [23] can also be applied in localization against wormhole attacks. SeRLoc and HiRLoc, however, cannot obtain satisfied localization performance as some attacked locators may still be undetected, and [23] does not suit for the scenario when many locators are attacked. SLAW proposed in this paper applies a novel mechanism to achieve higher performance without using extra hardware such as directional antennae required in SeRLoc and HiRLoc.

III. SYSTEM MODEL

A. Network Model

We assume that three types of nodes are deployed in the network: locators, sensors, and attackers. The locators have their locations known in advance (by manual deployment or GPS devices). Each locator has its own unique identification. The sensors does not know its location and they can estimate their locations by measuring distances to neighboring locators via message exchanges. The attackers exist in pairs colluding with each other to launch a *wormhole attack*. We assume that the transmission range of the sensors, locators and attackers is $R_S$, $R_L$ and $R_A$ respectively. For simplicity of description, we assume $R_S \leq R_L \leq R_A$, as shown in Figure 1. Note that the secure localization scheme proposed in this paper works well in other cases where $R_S$, $R_L$ and $R_A$ vary different. For the communication between two colluding attackers, however, their communication range is unlimited as they can communicate with each other using certain communication technique.

We also assume that the communication channel is not ideal. Even within the transmission range, a packet may be lost due to the transmission collision.

When the sensor needs self-localization, it broadcasts a location request message $Loc\_req$ to its neighboring locators.
Upon receiving the requesting message, each neighboring locator replies an acknowledgement message Loc_ack to the sensor. The sensor will use the received Loc_ack messages to build the set of its neighboring locators. The sensor can estimate the distances to all the locators based on the Loc_ack message by using the RSSI or ToA methods and estimate its location using the maximum likelihood estimation (MLE) approach [43]. Further more, the sensor measures the response time of each locator, which will be used to counter the locator’s random delay at the MAC layer.

**B. Attack Model**

We consider an adversarial environment where the localization procedure of the sensor may be attacked by a wormhole attack. During the wormhole attack, one attacker sniffs packets at one point in the network, forwards them via the wormhole link to another point of the network. We assume that the wormhole link is bi-directional and symmetrical so that the packets could be transmitted via either direction and no region is attacked by more than one wormhole simultaneously. Note that if the length of the wormhole link is less than $R_A$, then both attackers will be within the transmission area of each other such that the packet transmitted by one attacker can be received by the other attacker, resulting in endless packet transmission loop. To exclude this exceptional scenario, we assume the length of the wormhole link is larger than $R_A$. In order to make the wormhole attack more general, we assume that the attackers can randomly change their transmission powers for the packet retransmissions; they can also randomly drop off part or all of the packets they have overheard. However, we do not consider the case that the attackers can intentionally drop off certain types, or modify certain fields, of received packets. This is because we treat the wormhole attackers as external attackers which cannot acquire the content, such as the type of the packet, or modify the content, such as the recorded time stamp, of any overheard packet. The case that the attackers act as internal attackers that can break through the system’s authentication protection is out of the discussion of this paper.

Figure 1 shows that if the sensor $S$ uses the RSSI method in the localization, the wormhole can forward the packets from the locators $L_4$, $L_5$ and $L_6$ to $S$. $S$ will obtain the same distance measurement $d_0$ instead of the actual distances $d_0'$ and $d_0''$, as the RSSIs from $L_4$, $L_5$ and $L_6$ just reflect the propagational attenuations from $A_2$ to $S$. However, if $S$ uses the ToA method in the localization, it is totally different. Take an example of the locator $L_5$, when $L_5$ receives the Loc_req message from $S$ through the wormhole link, it transmits a Loc_ack message to $S$. As the transmission time in the wormhole link can be ignored, the time of arrival is introduced in two segments of the transmission path, from $L_5$ to $A_1$ and from $A_2$ to $S$. Therefore, after receiving the message, $S$ can calculate the distance from itself to $L_5$ as $d_0 + d_5$, instead of the actual distance $d_5'$. Similarly, $S$ can calculate the distances to $L_4$ and $L_6$ as $d_0 + d_4$ and $d_0 + d_6$, respectively, instead of the actual distances $d_4'$ and $d_6'$. Note that the neighboring locators of $S$ may include locators outside the transmission range of the sensor due to the existence of the wormhole link. Obviously, when $S$ receives messages relayed by the wormhole, it will use false distance measurements for the self-localization. We can also see that, for packets traversing two paths from a locator, say $L_5$, to $S$, the one going through the wormhole link, i.e., $L_5 \rightarrow A_1 \rightarrow A_2 \rightarrow S$, will take a longer delay to reach $S$ than the one going directly from $L_5$ to $S$.

Upon the view of the sensor, the locators within the sensor’s vicinity are classified as the following categories due to the existence of wormhole attack:

**Definition 1. Neighboring locator:** The locators which can communicate with the sensor, either via the wormhole link or not, are defined as the neighboring locators (N-locators) of the sensor.

**Definition 2. Valid locator:** The neighboring locators, which can communicate with the sensor directly, are called valid locators (V-locators) because their messages can be directly received by the sensor to obtain correct distance measurements. The distance between each V-locator and the sensor is less than $R_L$.

**Definition 3. Dubious locator:** The locators, which are within the transmission range of the attacker and can communicate with the sensor via the wormhole link, are defined as dubious locators (D-locators) since their distance measurements can negatively affect the localization procedure. The distance between each D-locator and the attacker is less than $R_L$.

We denote the set of N-locators, V-locators, D-locators as $\mathcal{L}_N$, $\mathcal{L}_V$ and $\mathcal{L}_D$, respectively. For the sample network shown in Fig 1, for the sensor $S$, $\mathcal{L}_N = \{L_1, L_2, L_3, L_4, L_5, L_6\}$, $\mathcal{L}_V = \{L_1, L_2, L_3, L_4\}$ and $\mathcal{L}_D = \{L_4, L_5, L_6\}$. It is obvious that $\mathcal{L}_N = \mathcal{L}_V \cup \mathcal{L}_D$ Note that $L_7$ does not belong to any set since it is not a N-locator of $S$. We also denote $\mathcal{D}_R(u)$ as a disk centered at $u$ with radius $R$. 

![Fig. 1. Wormhole attack in the range-based localization.](image-url)
IV. Secure Localization Scheme Against Wormhole Attacks

The wormhole attack can disrupt the localization procedure of the sensor only if the sensor enters the transmission area of either attacker and communicates with the locators via the wormhole link. Two different types of wormhole attacks, named Class 1 wormhole attack (Figure 3(a)) and Class 2 wormhole attack (Figure 3(b)), are defined as follows:

**Definition 4. Class 1 wormhole attack:** The sensor is under class 1 wormhole attack when the message it transmits can arrive at itself via the wormhole link. That is, the distance between the sensor and one of the attackers is less than \( R_A \) and the distance between the sensor and the other attacker is larger than \( R_S \).

**Definition 5. Class 2 wormhole attack:** The sensor is under class 2 wormhole attack when it can exchange messages with some locators via the wormhole link, but cannot receive its own message. That is, the distance between the sensor and one of the attackers is less than \( R_S \), while the distance between the sensor and the other attacker is larger than \( R_A \).

Without special treatments, the localization process would be deteriorated when the sensor is under a wormhole attack. Therefore, the critical task for the sensor is to detect the existence of the wormhole attack and to identify the dubious locators to achieve secure localization. The proposed SLAW is shown in Algorithm 1 which includes the following three phases:

- **Wormhole Attack Detection:** The sensor detects whether it is under a wormhole attack using wormhole detection schemes.
- **Neighboring Locators Differentiation:** When a wormhole attack is detected, the sensor identifies its N-locators as D-locators and V-locators.
- **Secure Localization:** After identifying the D-locators, the sensor uses valid locators to conduct the MLE localization with the correct distance measurements.

**Algorithm 1 SLAW scheme**

1: When the sensor receives messages from neighboring locators, it runs wormhole attack detection process.
2: **if** the wormhole attack is detected **then**
3: The sensor runs neighboring locators differentiation process.
4: **end if**
5: The sensor runs secure localization process.

A. Wormhole Attack Detection

In a hostile WSN where wormhole attacks exist, the sensor has to detect whether it is attacked by a wormhole before conducting the self-localization. The sensor broadcasts a \( \text{Loc}_\text{req} \) message and waits for the reply messages, i.e., the \( \text{Loc}_\text{ack} \) messages from its neighboring locators. When receiving the \( \text{Loc}_\text{req} \) message, each locator responds a \( \text{Loc}_\text{ack} \) message.

The sensor will use the received \( \text{Loc}_\text{ack} \) messages to build the set of its neighboring locators. It also measures the distance to each neighboring locator from the received \( \text{Loc}_\text{ack} \) message. Further more, the sensor measures the response time of each locator.

As the response time of the locator is affected by the random delay at the MAC layer of the locator, we adopt the approach in [44] to countervail this random delay: As shown in Figure 2, when broadcasting the \( \text{Loc}_\text{req} \) message, the sensor records the local time \( T_0 \). Every locator gets the local time \( T_1 \) by time-stamping the message at the MAC layer (i.e., the time when the message is received at the MAC layer) instead of time-stamping the message at the application layer. Similarly, when responding the \( \text{Loc}_\text{ack} \) packet, the locator puts the local time \( T_2 \) at the MAC layer, both \( T_1 \) and \( T_2 \) are attached in the \( \text{Loc}_\text{ack} \) packet. When receiving the \( \text{Loc}_\text{ack} \) packet, the sensor gets its local time \( T_3 \), and calculates the response time of the locator as \((T_3-T_0)-(T_2-T_1)\). In this procedure, only the random delay at the MAC layer of the locators is eliminated from the response time, while the delay affected by attackers still exists.

When building the set of neighboring locators, the sensor may observe some abnormalities occur due to the existence of the wormhole attack. The following four properties can be used to detect the existence of the wormhole attack.

**Node’s self-exclusion property:** Each node can not receive any message transmitted by itself in a loop-free path.

**Detection scheme D1 based on node’s self-exclusion property:** When the sensor is under the class 1 wormhole attack like Figure 3(a), it can detect the wormhole attack simply as follows: When the sensor \( S \) broadcasts the \( \text{Loc}_\text{req} \) message, as \( A_1 \) lies in \( D_{R_S}(S) \), it can receive the message from \( S \), and then relayed through the wormhole link to \( A_2 \), after relayed by \( A_2 \), this message can arrive at \( S \) as \( S \) lies in \( D_{R_S}(A_2) \). Similarly, the broadcasted \( \text{Loc}_\text{req} \) message may also travel from \( A_2 \) through the wormhole link to \( A_1 \) and then being received by \( S \). Therefore, the sensor can determine that it is under a wormhole attack if it receives the \( \text{Loc}_\text{req} \) message sent by itself.

**Packet unduplication property:** Each node can receive at most one copy of the same message from one of its neighboring nodes.

**Detection scheme D2 based on packet unduplication property:** As shown in Figure 3(b), a dubious locator \( L_4 \) may lie in the common area of the regions \( D_{R_S}(S) \) and \( D_{R_S}(A_1) \). When \( L_4 \)
responses, $S$'s $Loc_{req}$ message, the $Loc_{ack}$ messages can be received by $S$ twice, one directly from $L_4$ and the other from $A_2$ which is replayed from $A_1$ to $A_2$ through the wormhole link. Therefore, if $S$ receives more than one message from the same neighboring locator for each request, it determines that it is under a wormhole attack.

**Node's spatial constraint property:** The measured distance between two neighboring nodes cannot be larger than $R_S$.

**Detection scheme D3 based on node's spatial constraint property:** The measured distance between the sensor and its neighboring locator can be larger than $R_S$ when the wormhole attack exists. Therefore, the sensor can check whether any measured distance to its neighboring locators is larger than $R_S$. If one measured distance is found larger than $R_S$, the sensor considers a wormhole attack exists.

**Neighboring nodes' spatial constraint property:** Each node cannot receive messages from its two neighboring nodes simultaneously if the distance between them is larger than $2R_S$.

**Detection scheme D4 based on neighboring nodes' spatial constraint property:** As shown in Figure 3(b), $L_2$ is a locator which lies farther than $2R_S$ away from $L_8$. After receiving the $Loc_{req}$ message from neighboring locators, $S$ will check whether the distance between any two locators is larger than $2R_S$. If $S$ detects that the distance between $L_2$ and $L_4$ is larger than $2R_S$, it derives that it is under a wormhole attack.

The wormhole detection procedure is shown in Algorithm 2. After receiving the $Loc_{ack}$ messages from its neighboring locators, the sensor can use the wormhole detection scheme D1 to detect class 1 wormhole attack and use the wormhole detection schemes D2, D3 or D4 to detect class 2 wormhole attack. If the sensor detects a wormhole attack, it uses the neighboring locators differentiation to identify the dubious locators; otherwise, it conduct the secure localization process. Note that although this differentiation scheme may not be able to identify all D-locators in certain scenarios, the localization using remaining locators after the differentiation can achieve high location estimation, which is shown in the simulation section.

Since the algorithms that deal with class 1 and class 2 wormhole attacks are independent, the sensor needs to determine the type of the wormhole attack after the wormhole attack detection. However, if considering the general network model that packet loss exists during the message exchanges because of either the packet transmission collisions or the packet drop-off by the wormhole, the sensor may detect the type of the wormhole attack incorrectly. That is, when the sensor is under a class 1 wormhole attack, it may fail to detect the class 1 wormhole attack with the detection scheme D1 but detect a class 2 wormhole attack with the detection schemes D2, D3 or D4. The way to mitigate the impact of this mistake is that, when the sensor receives packets from itself or from any neighboring locator for three times (this scenario happens only when the sensor is under the class 1 wormhole attack, as $L_4$ in Figure 3(a)) during the neighboring locators differentiation, it will rectify that it is under the class 1 wormhole attack instead of the class 2 wormhole attack and re-conducts the algorithm for the class 2 wormhole attack.

**Algorithm 2 Wormhole attack detection**

1: Broadcast a $Loc_{req}$ message.
2: Wait for the $Loc_{ack}$ messages to measure the distance and calculate the response time of each locator.
3: if detect the wormhole attack based on scheme D1 then
4: Class 1 wormhole attack is detected.
5: else if detect the wormhole attack based on schemes D2, D3 or D4 then
6: Class 2 wormhole attack is detected.
7: else
8: No wormhole attack is detected.
9: end if

**B. Neighboring Locators Differentiation**

The core idea of these neighboring locators differentiation algorithms is to allow all locators to build their so-called...
conflicting sets, which are based on the abnormalities of the Beacon message exchanges among neighboring locators. By analyzing the conflicting sets of neighboring locators, the sensor can differentiate dubious locators from valid locators. The conflicting set is defined as follows:

Definition 6. Conflicting set: The conflicting set of a locator $L_i$, denoted as $C(L_i)$, contains all the abnormal neighboring locators of the locator $L_i$, including (1) $L_i$ itself if it can receive the Beacon message sent by itself, (2) neighboring locators that are within the transmission range of $L_i$ but send several copies of the same Beacon message through different paths to $L_i$, and (3) neighboring locators that are outside the transmission range of $L_i$ but whose Beacon messages can be received by $L_i$.

Based on the periodical Beacon message exchanges with its neighboring locators, each locator can build its conflicting set. When a locator detects the Beacon message abnormality, it will put the locator (the source node of this Beacon message) into its conflicting set. When such a locator receives a Loc_req message from the sensor, it responds a Loc_ack message including its conflicting set to the sensor.

The following theorem shows the relationship among the locator $L_i$, its conflicting set $C(L_i)$, and $D_{R_i}(A_1)$, $D_{R_i}(A_2)$, $D_{R_i}(A_3)$ and $D_{R_i}(A_4)$:

**Theorem 1.** Given a network shown in Figure 4, (1) if $L_i$ lies in $D_{R_i}(A_2)$ \ $D_{R_i}(A_1)$, all the locators in $C(L_i)$ lie in $D_{R_i}(A_1)$; (2) if $L_i$ lies in $D_{R_i}(A_1)$ \ $D_{R_i}(A_2)$, all the locators in $C(L_i)$ lie in $D_{R_i}(A_2)$; (3) if $L_i$ lies in $D_{R_i}(A_1)$ \ $D_{R_i}(A_2)$, all the locators in $C(L_i)$ lie in $D_{R_i}(A_1)$ \ $D_{R_i}(A_2)$.

**Proof:** For the scenario without packet loss:

(1) Consider a locator $L_j$ in $D_{R_i}(A_1)$, its Beacon message can be received by all its neighboring locators. As $L_j$ lies in $D_{R_i}(A_2)$ \ $D_{R_i}(A_1)$, it can calculate the distance between $L_j$ and $L_i$ after receiving the Beacon message from $L_j$. If the distance is larger than $R_L$, $L_i$ derives that it receives a packet from a locator outside $D_{R_i}(L_i)$, and then, $L_j \in C(L_i)$; if the distance is less than $R_L$, $L_i$ lies in $D_{R_i}(L_i)$ and a direct transmission path between $L_i$ and $L_j$ exists in addition to the transmission path through the wormhole link. Consequently, $L_i$ can receive the same message from $L_j$ for more than once. Therefore, $L_j \in C(L_i)$. Moreover, for any other locator $L_k \notin D_{R_i}(A_1)$, its message cannot arrive at $L_i$ through the wormhole link, there is no abnormality of message exchanges between $L_i$ and $L_k$. Therefore, all locators in $C(L_i)$ lie in $D_{R_i}(A_1)$.

(2) Similar to case (a), if $L_i$ lies in $D_{R_i}(A_1)$ \ $D_{R_i}(A_2)$, all the locators in $C(L_i)$ lie in $D_{R_i}(A_2)$.

(3) If $L_i$ lies in $D_{R_i}(A_1)$ \ $D_{R_i}(A_2)$, it can receive the Beacon messages from all the locators in $D_{R_i}(A_1)$ \ $D_{R_i}(A_2)$ via the wormhole link. For each locator $L_j \in D_{R_i}(A_1)$ \ $D_{R_i}(A_2)$, $L_i$ can detect the abnormality by either receiving the message for more than once or receiving the message beyond the transmission range. Therefore, $L_j \in C(L_i)$. If $L_i$ lies in $D_{R_i}(A_1)$ \ $D_{R_i}(A_2)$, it can also receive the message transmitted by itself, then $L_i \in C(L_i)$. Meanwhile, for any other locator $L_k \notin D_{R_i}(A_1)$ \ $D_{R_i}(A_2)$, it cannot be in $C(L_i)$ as its Beacon message cannot received by $L_i$ via the wormhole link. Thus, all the locators in $C(L_i)$ lie in $D_{R_i}(A_1)$ \ $D_{R_i}(A_2)$.

As shown in Fig 4, the locators $L_1, L_2, L_3$ lie in $D_{R_i}(A_2)$ \ $D_{R_i}(A_1)$, the locator $L_4$ lies in $D_{R_i}(A_1)$ \ $D_{R_i}(A_2)$, and the locators $L_5, L_6, L_7, L_8$ lie in $D_{R_i}(A_1)$ \ $D_{R_i}(A_2)$. Theorem 1 illustrated in Fig. 4. Illustrations for building the conflicting sets.

The sensor $S$ can build a conflicting matrix of its $n$ neighboring locators as follows:

$$M_c = \begin{pmatrix} m_{11} & m_{12} & \cdots & m_{1n} \\ m_{21} & m_{22} & \cdots & m_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ m_{n1} & m_{n2} & \cdots & m_{nn} \end{pmatrix}$$

Where $m_{ij} = \begin{cases} 1, & \text{if } L_j \in C(L_i) \\ 0, & \text{if } L_j \notin C(L_i) \end{cases}$.

Due to the packet loss, the conflicting matrix is not symmetric, e. g., for some $i, j, m_{ij} \neq m_{ji}$. To make the confliction relationship among the locators more reliable, we adopt the conservative strategy to handle the conflicting set. For the conflicting matrix, the sensor conducts $m_{ij} = m_{ji} = (m_{ij} + \bar{m}_{ji})/2$. That is, if $L_j \in C(L_i)$, the sensor will consider the relationship as valid only if $L_j \in C(L_i)$. For instance, the locator $L_6$ in Figure 4 may include $L_3$ into its conflicting set, but $L_6$ cannot be in the conflicting set of $L_3$ as $A_1$ is outside the transmission range of $L_6$. So the sensor will consider it as invalid.
After this operation, the result of the conflicting sets for the locators can be summarized as follows: Given a sample network as shown in Figure 4, (1) if $L_i$ lies in $D_R(A_2) \setminus D_R(A_1)$, all the locators in $C(L_i)$ lie in $D_R(A_1)$; (2) if $L_i$ lies in $D_R(A_1) \setminus D_R(A_2)$, all the locators in $C(L_i)$ lie in $D_R(A_2)$; (3) if $L_i$ lies in $(D_R(A_1) \cap D_R(A_2)) \cap (D_R(A_1) \cup D_R(A_2))$, all the locators in $C(L_i)$ lie in $D_R(A_1) \cup D_R(A_2)$. 

1) Class 1 Wormhole Attack: When the sensor is under a class 1 wormhole attack as shown in Figure 3(a), all the locators which can exchange messages with the sensor via the wormhole link are D-locators because they will bring the sensor incorrect distance measurements. To identify the V-locators and D-locators, the sensor needs to check the conflicting sets of its neighboring locators.

The procedure of neighboring locators differentiation under the class 1 wormhole attack is described in Algorithm 3.

**Algorithm 3** Neighboring locators differentiation under the class 1 wormhole attack

1: Each locator periodically exchanges the *Beacon* messages with all its neighboring locators and builds its conflicting set based on the received *Beacon* messages.
2: When receives the *Loc_req* message from the sensor, each locator replies a *Loc_ack* message including its conflicting set to the sensor.
3: The sensor builds the conflicting matrix and conducts the mathematical operation.
4: for each neighboring locator $L_i$ do
5: if $C(L_i) \neq \emptyset$ then
6: Add $L_i$ into $L_D$;
7: else
8: Add $L_i$ into $L_V$.
9: end if
10: end for

Each locator periodically exchanges the *Beacon* messages with all its neighboring locators, based on which it can build its conflicting set. Before conducting self-localization, the sensor broadcasts a *Loc_req* message to all its neighboring locators. When receiving the *Loc_req* message from the sensor, each locator replies the *Loc_ack* message including its conflicting set to the sensor. The sensor builds the conflicting matrix and conducts the mathematical operation as described above. The sensor checks the conflicting set of each neighboring locator, if the conflicting set is not empty, the locator is considered a D-locator; otherwise, if the conflicting set is an empty set, the locator is considered a V-locator.

2) Class 2 Wormhole Attack: As shown in Figure 3(b), when the sensor is under a class 2 wormhole attack, only the locators in $D_R(A_1)$ are D-locators. To identify all D-locators in this scenario, our algorithm adopts the following identification schemes.

**Identification scheme II:** When the sensor is under a class 2 wormhole attack, the locators which are detected by the sensor with the packet unduplication property are considered as D-locators. As shown in Figure 3(b), $L_4$ lies in $D_R(S) \cap D_R(A_1)$.

If it is detected by $S$ with the packet unduplication property, $S$ determines that $L_4$ is a D-locator.

**Identification scheme I2:** When under a class 2 wormhole attack, if the sensor has two neighboring locators the distance between which is larger than $2R_L$, one of the two locators is a D-locator while the other is a V-locator. As the message exchanged between the sensor and the D-locator travels through the wormhole link, the response time is larger than that of the V-locator. Therefore, the sensor considers the locator with a shorter response time as a V-locator, and the other locator is labeled as a D-locator. As shown in Figure 3(b), the distance between $L_2$ and $L_8$ is larger than $2R_L$, the sensor determines that $L_2$ (with a shorter response time) is a V-locator and $L_8$ is a D-locator (with a longer response time).

**Theorem 2.** When the sensor is under a class 2 wormhole attack and the length of the wormhole link is larger than $R_A + R_L$, if $\exists L_i \notin L_D$ such that $C(L_i) \neq \emptyset$, then $\forall L_j \in C(L_i)$, $L_j \in L_D$.

**Proof:** As shown in Figure 4, if the length of the wormhole link is larger than $R_A + R_L$, then $D_R(A_2) \cap D_R(A_1) = \emptyset$. When the sensor is under a class 2 wormhole attack, since $\forall L_i$ such that $C(L_i) \neq \emptyset$, $L_i$ must lie in $D_R(A_1) \cup D_R(A_2)$. As $L_i \notin L_D$, i.e., $L_i \notin D_R(A_1)$, $L_i$ can only lie in $D_R(A_2) \setminus D_R(A_1)$. Moreover, as $D_R(A_2) \cap D_R(A_1) = \emptyset$, we can obtain that $L_i$ lies in $D_R(A_2) \setminus D_R(A_1)$. According to the result of the conflicting sets among the locators, as $L_i$ lies in $D_R(A_2) \setminus D_R(A_1)$, all locators in $C(L_i)$ lie in $D_R(A_1)$. Therefore, $\forall L_j \in C(L_i)$, $L_j \in L_D$.

**Identification scheme I3:** When the sensor detects that a V-locator and a D-locator using identification scheme I2, the V-locator $L_i$ cannot belong to $L_D$. If $L_i$’s conflicting set $C(L_i)$ is not empty, the sensor considers all locators in $C(L_i)$ as D-locators.

**Theorem 3.** When the sensor is under a class 2 wormhole attack and the length of the wormhole link is larger than $R_A + R_L$, if $\exists L_i \notin L_D$ such that $C(L_i) \neq \emptyset$, then $\forall L_j$ such that $L_j \in C(L_i)$, $L_j \in L_D$.

**Proof:** As shown in Figure 4, if the length of the wormhole link is larger than $R_A + R_L$, then $D_R(A_2) \cap D_R(A_1) = \emptyset$. As $L_i \notin L_D$ and $C(L_i) \neq \emptyset$, $L_i$ must lie in $D_R(A_2) \setminus D_R(A_1)$ according to Theorem 2. When the sensor is under a class 2 wormhole attack. As $L_i \in C(L_i)$, $L_j$ cannot lie in $D_R(A_2) \setminus D_R(A_1)$, otherwise, if $L_j$ lies in $D_R(A_2) \setminus D_R(A_1)$, all the locators in $C(L_j)$, including $L_i$, lie in $D_R(A_1)$, which contradicts to the condition that $L_i$ lies in $D_R(A_2) \setminus D_R(A_1)$. Moreover, as $C(L_i) \neq \emptyset$, $L_i$ must lie in $D_R(A_2) \setminus D_R(A_1)$. Due to $D_R(A_1) \cap D_R(A_2) = \emptyset$, $L_j$ can only lie in $D_R(A_1) \setminus D_R(A_2)$, which means $L_j \in L_D$.

**Identification scheme I4:** When the sensor detects that a V-locator and a D-locator using identification scheme I2, the V-locator $L_i$ cannot belong to $L_D$. If $L_i$’s conflicting set $C(L_i)$ is not empty, the locator which includes $L_i$ into its conflicting set will be considered as a D-locator.
When the sensor detects that it is under the class 2 wormhole attack, it can identify all the D-locators based on the above identification schemes. The procedure for identifying the D-locators is shown in Algorithm 4.

**Algorithm 4** Neighboring locators differentiation under the class 2 wormhole attack

1. Each locator periodically exchanges the Beacon messages with all its neighboring locators and builds its conflicting set based on the received Beacon messages.
2. When receiving the Loc_req message from the sensor, each locator replies the Loc_ack message including its conflicting set to the sensor.
3. The sensor builds the conflicting matrix and conducts the mathematical operation.
4. The sensor conducts schemes I1, I2, I3 and I4 to build \( L_D \).
5. For each neighboring locator \( L_i \notin L_D \) do
6. Add \( L_i \) into \( L_V \).

Each locator periodically exchanges the Beacon messages with all its neighboring locators, based on which it can build its conflicting set. Before conducting self-localization, the sensor broadcasts a Loc_req message to all its neighboring locators. When receiving the Loc_req message from the sensor, each locator replies the Loc_ack message including its conflicting set to the sensor. The sensor builds the conflicting matrix and conducts the mathematical operation as described above. The sensor then uses the identification schemes I1, I2, I3 and I4 to identify all dubious locators. After that, for each neighboring locator that is not marked as a D-locator, it is considered as a V-locator. Although identification schemes I3 and I4 may incorrectly identify some V-locators as D-locators as the sensor cannot confirm that the length of the wormhole link is larger than \( R_A + R_L \), the negative effect is limited as shown in the simulation results.

### C. Secure Localization

After wormhole attack detection and neighboring locators differentiation, the sensor can identify some valid locators. However, among the dubious locators, there may exist some locators which are also valid locators, such as \( L_3 \), \( L_4 \) and \( L_5 \) in Figure 3(a) and \( L_4 \) in Figure 3(b). Therefore, their distance measurements can be used into localization. As the sensor may receive multiple copies of the same message from these locators, it will consider the one with the shortest response time as the correct distance measurement. For the distance measurements which are larger than \( R \) due to the wormhole attack or measurement error, the sensor filters them out before localization. At the end, the valid distance measurements of the valid locators are used in the MLE localization.

The MLE localization works as follows: Assume that the sensor has obtained valid distance measurements from \( m \) valid locators. The coordinates of the \( m \) locators are \((x_1, y_1), (x_2, y_2), (x_3, y_3), ..., (x_m, y_m)\) respectively, and the distance measurements from the \( m \) locators to the sensor are \( d_1, d_2, d_3, ..., d_m \). Then, the location of the sensor \((x, y)\) satisfies:

\[
\begin{align*}
(x - x_1)^2 + (y - y_1)^2 &= d_1^2 \\
(x - x_2)^2 + (y - y_2)^2 &= d_2^2 \\
&\vdots \\
(x - x_m)^2 + (y - y_m)^2 &= d_m^2
\end{align*}
\]

By subtracting the last equation from each of the rest ones in Eq. (1), we can obtain the following equations represented as a linear equation \( AX = b \), where

\[
A = \begin{bmatrix}
2(x_1 - x_m) & 2(y_1 - y_m) \\
2(x_2 - x_m) & 2(y_2 - y_m) \\
\vdots & \vdots \\
2(x_{m-1} - x_m) & 2(y_{m-1} - y_m)
\end{bmatrix}, \quad X = \begin{bmatrix} x \\ y \end{bmatrix}, \quad b = \begin{bmatrix}
x_1^2 - x_m^2 + y_1^2 - y_m^2 - d_1^2 + d_m^2 \\
x_2^2 - x_m^2 + y_2^2 - y_m^2 - d_2^2 + d_m^2 \\
\vdots \\
x_{m-1}^2 - x_m^2 + y_{m-1}^2 - y_m^2 - d_{m-1}^2 + d_m^2
\end{bmatrix}
\]

The location of the sensor is finally calculated as

\[
X = (A^T A)^{-1} A^T b
\]

### V. Simulation Results

In this section, we present the simulation results to demonstrate the effectiveness of the SLAW. Particularly, we evaluate the performance of the SLAW when the length of the wormhole link varies. We model the general network model as follows: when the distance \( d \) between two nodes is less than \( a r \), there is no packet loss; when \( d \) is within \([a r, r]\), the probability of packet loss is \( 2ar - d \), where \( 0 \leq a \leq 1 \). Thus, if a node lies outside the transmission range of a sender, this node cannot receive message from the sender. We also assume the wormhole attack will drop the received messages with a probability \( \omega \) (0 \( \leq \omega \leq 1 \)). The network settings are as following: the locators are deployed independently with a density \( \rho = 0.006/m^2 \) (with the average degree around 4); the label \( L/R_A \) of the \( x \) axis denotes the ratio of the length of the wormhole link (i.e., the distance between two attackers) to the transmission range of the attacker; the transmission ranges of the sensors, locators and attackers are set as \( R_S = 13m, R_L = 14m \) and \( R_A = 15m \) respectively; \( \alpha = 0.75 \) and \( \omega = 0.2 \). For simplicity, we assume that the measurement error of the distance follows a normal distribution \( N(\mu, \sigma^2) \) with the mean \( \mu = 0 \) and the standard deviation \( \sigma \) is within a threshold 0.5.

We repeat each simulation for 20,000 times by randomly deploying locators with the Poisson distribution. The successful probabilities of the wormhole attack detection process and the secure localization process of SLAW are compared with the one without any wormhole attack detection procedure (labeled as “Without detection”) and other two secure localization approaches: SeRLoc [8] and Consistency [23]. The localization is considered as successful only if \( d_{err1} \leq d_{err2} + f_{err} * R_S \), where \( d_{err1} \) (and \( d_{err2} \)) denotes the localization error with (and
without) using the secure localization scheme, \( f_{tol} \) is the factor of localization error tolerance (0.1 in our simulations).

Figure 5 shows the performance comparison of SLAW and SeRLoc scheme [8] in terms of the probability of successful wormhole attack detection. For the RSSI-based localization, SLAW outperforms SeRLoc when \( L/R_A \leq 2 \) while there is no difference when \( L/R_A > 2 \). This is because SLAW with the RSSI-based localization only improves the wormhole attack detection when the sensor is under the class 1 wormhole attack, which exists only when \( L/R_A \leq 2 \). For the ToA-based localization, SLAW has a higher detection probability for all ranges of \( L/R_A \). It shows that SLAW provides successful detection probability at least 70% while SeRLoc is about 61% in the worst case. When \( L/R_A \) is large enough, the probability of successful wormhole attack detection of SLAW approximates 90% (98% for ToA-based secure localization).

Upon detecting the wormhole attack, the sensor adopts one of the two differentiation algorithms to identify the dubious locators according to the type of the wormhole attack. However, the sensor may make false alarm, i.e., it may identify
incorrectly that it is under the class 2 wormhole attack while it is actually under the class 1 wormhole attack. The reason that false alarms occur is that the sensor may miss some packets due to the transmission collisions or the random drop-offs. Figure 6 demonstrates the probability of false alarm when the sensor is under the wormhole attack. It shows that the misidentification of the wormhole attack happens only when $L/R_A$ is less than $2R_A$ and the probability is at most 1.2%.

Figure 7 shows the performance of successful localization of SLAW, SeRLoc, Consistency and “Without detection” schemes. The SeRLoc scheme identifies D-locators using the sector uniqueness and communication range violation properties, then conducts self-localization based on the rest locators. The consistency scheme identifies the most inconsistent locator as a D-locator based on the consistency check of the estimation result. The performance of the “Without detection” scheme shows the severe impact of the wormhole attack on the localization. Among these schemes, SLAW obtains the best performance. The performance of SLAW and SeRLoc increases with the increase of $L/R_A$, while the performance of the consistency scheme is insensitive to the value changes of $L/R_A$. When $L/R_A$ is larger than 3, the probability of successful localization gets close to 100%.

Figure 8 shows the performance of successful localization of SLAW under different locator densities. It shows that the performance of SLAW improves greatly with the enlargement of locator density when the length of the wormhole link is less than $2R_A$. When the length of the wormhole link is larger than $2R_A$, however, it seems that the enlargement of locator density has no visible improvement.

VI. CONCLUSION AND FUTURE WORK

In this paper, we analyze the severe impacts of the wormhole attack on the localization in hostile wireless sensor networks. To tackle this secure problem, we propose a novel secure localization scheme SLAW which works well under a general system model. We also conduct simulations that demonstrate our scheme outperforms other existing schemes. In this paper, we only adopt the conservative strategy to handle the conflicting relationship among neighboring locators. In our future work, we will apply the topology inference theories to solve these conflicting relationships and make the conflicting sets of neighboring locators consistent and trustable. When a sensor is attacked by multiple wormhole attacks simultaneously, it will be very complicated and difficult to obtain secure localization. A potential solution is to separate the localization from the wormhole attack detection. That is, when multiple wormhole attacks are detected, the system can try to identify the locations of the attackers and then eliminate them. Thus, the other direction of our future work will focus on the detection of multiple wormhole attacks and the localization of the attackers.

ACKNOWLEDGMENT

This work is supported in part by grants PolyU 5236/06E, PolyU 5243/08E, PolyU 5253/09E, 1-ZV5N, ZJU-SKL ICT0903, NSFC 60873223, NSFC 90818010 and International Cooperative Project of Science and Technology Department of Zhejiang Province (2009C34002).

REFERENCES


