A Real-Time Multicast Routing Scheme for Multi-Hop Switched Fieldbuses

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Content



Demand



Background



Problem Definition and Complexity



Heuristic Algorithm



Evaluation



Related Work



Fieldbus is fundamentally different from the Internet, hence requires different solutions.

Specialized networks used in industrial, mining, medical, vehicular, avionic environments

Fieldbus:

Hard Real-Time

Periodic Stable Traffic

Bounded w/ Global Info

The Internet:

Best Effort

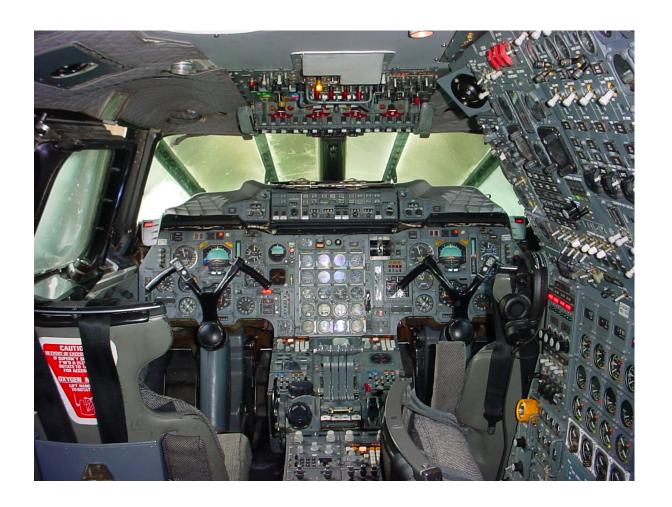
Random Bursty Traffic

Unbounded w/o Global Info



Fieldbus is evolving from shared medium to multi-hop switched due to scalability needs.

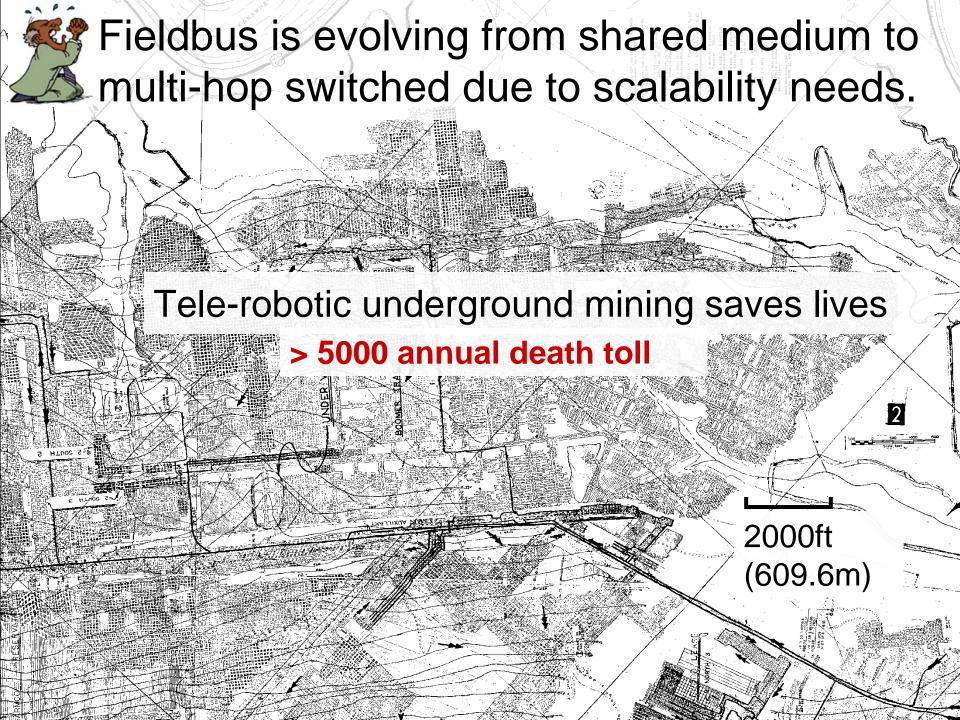
Concord 1976





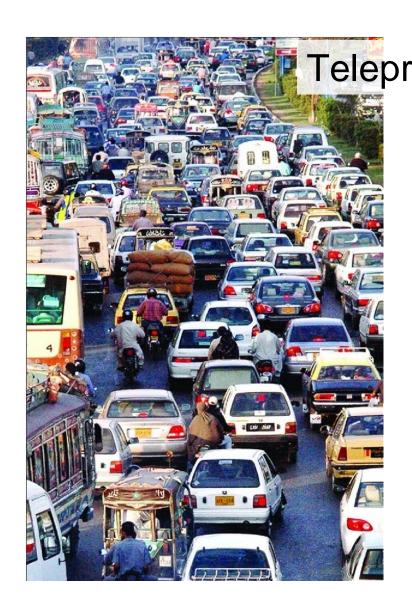
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Sieldbus is evolving from shared medium to multi-hop switched due to scalability needs.



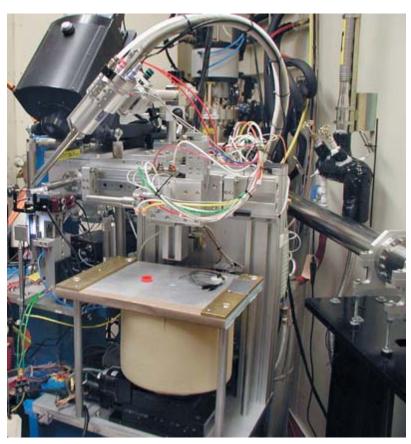




Fieldbus is evolving from shared medium to multi-hop switched due to scalability needs.

Robotic Manufacturing







Shared medium -> multi-hop switched: realtime multicast becomes a problem.

$$\dot{x}(t)_{n\times 1} = A_{n\times n} x(t)_{n\times 1} + B_{n\times m} u(t)_{m\times 1}$$
$$u(t)_{m\times 1} = -K_{m\times n} x(t)_{n\times 1}$$

Modern control assumes MIMO →
Real-Time Multicast btw
Sensors-Controllers-Actuators/Observers



Shared medium -> multi-hop switched: realtime multicast becomes a problem.

$$\dot{x}(t)_{n\times 1} = A_{n\times n} x(t)_{n\times 1} + B_{n\times m} u(t)_{m\times 1}$$
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Shared Medium Real-Time Multicast: Easy

Multi-Hop Switched Real-Time Multicast: ?





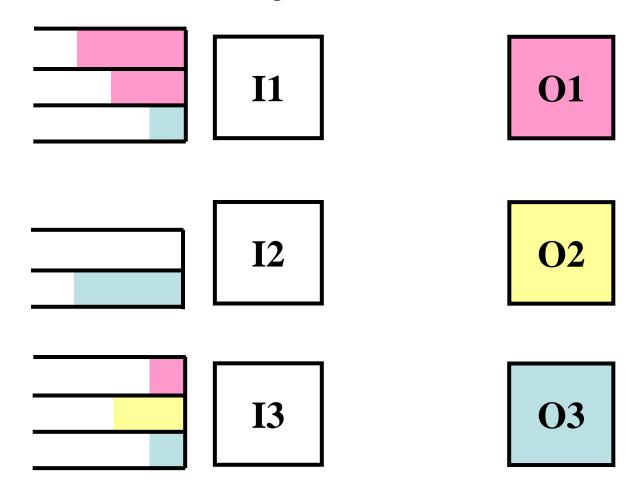
Input Ports



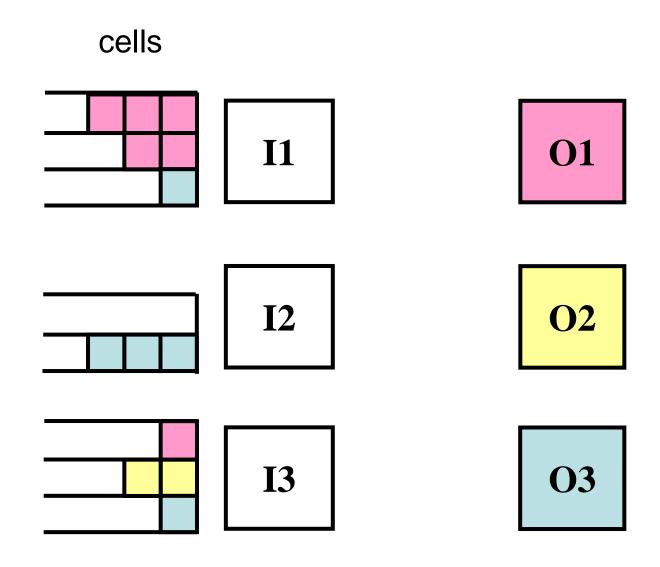
Output Ports I2



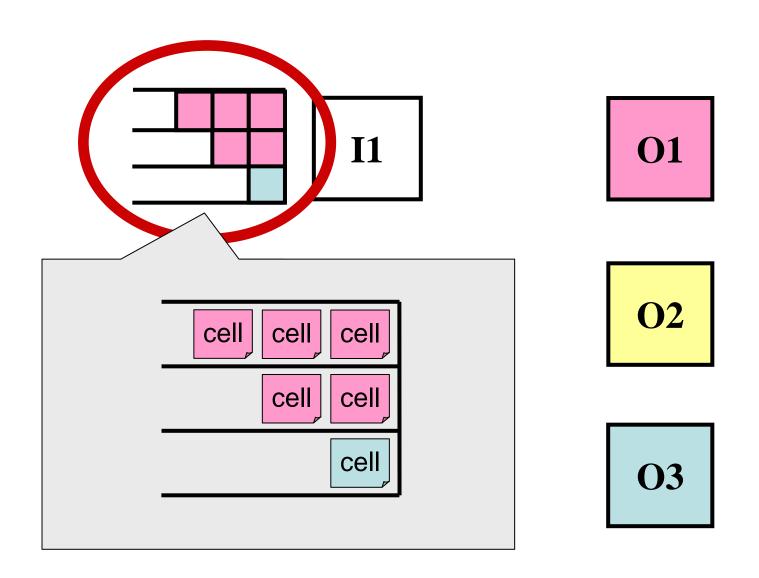
Per-Flow-Queueing







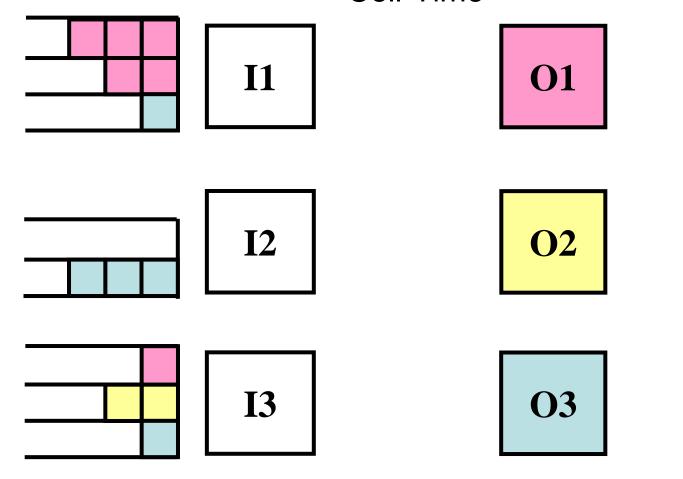




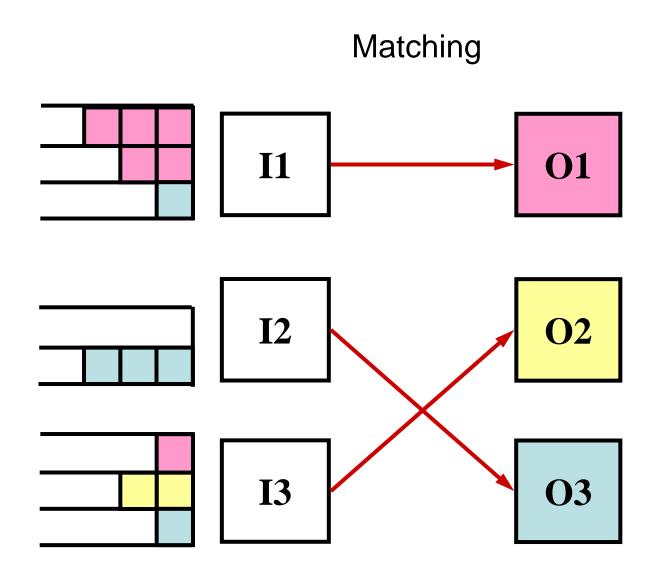
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De facto standard (real-time) fieldbus switch architecture: crossbar per-flow-q TDMA

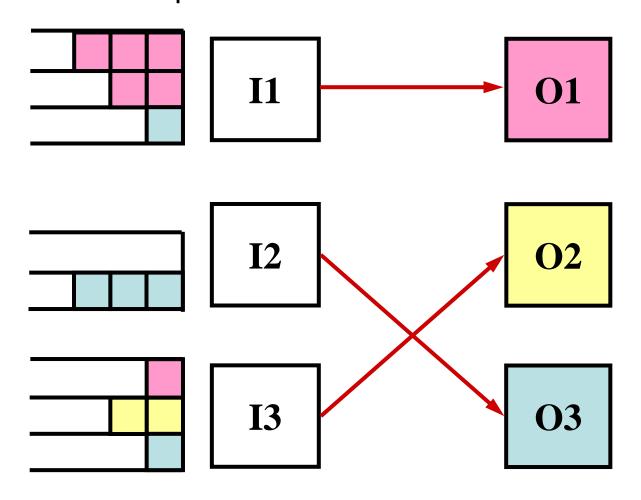
Synchronous periodic cell forwarding Cell-Time





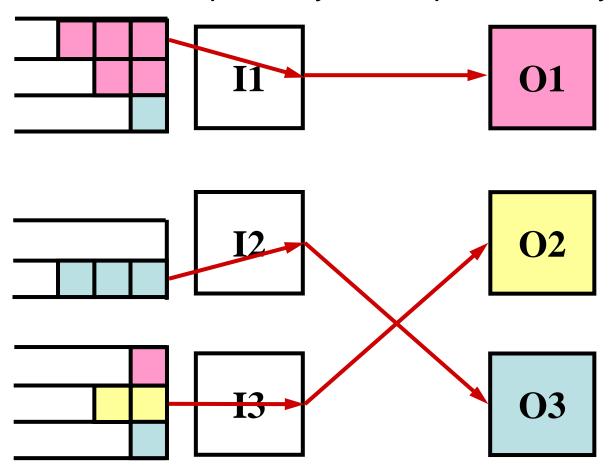


Why Matching? An input/output can only send/receive one cell per cell-time

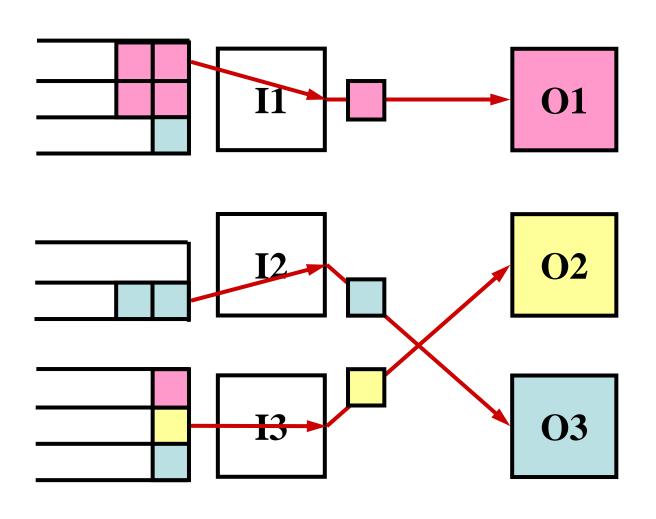




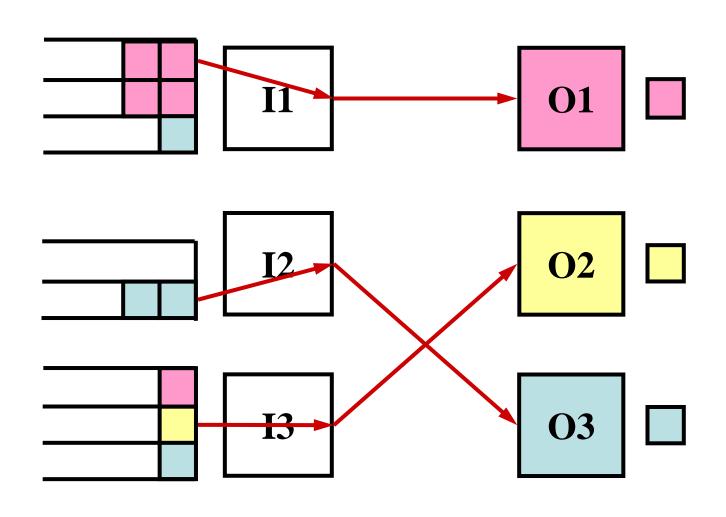
Internal Matching: if an input has multiple per-flow-q for the same output, only one is picked every cell-time.



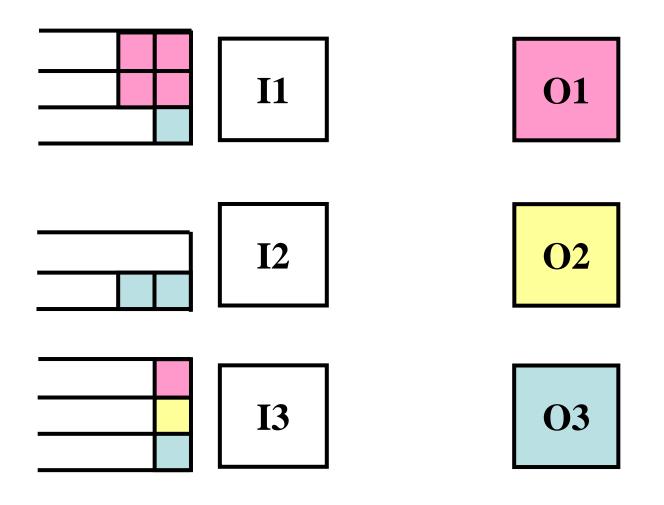








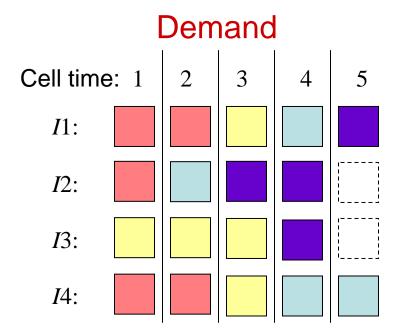


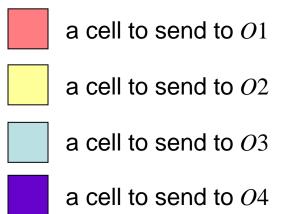




TDMA scheduling frame of M cell-time, e.g., M = 5

Fit all real-time flows' periods into frame, e.g., $(11, 3) \rightarrow (5, 2)$, i.e., (10, 4)





althe

Cell time: 1

*I*1:

*I*2:

*I*3:

*I*4:

De facto standard (real-time) fieldbus switch architecture: crossbar per-flow-q TDMA

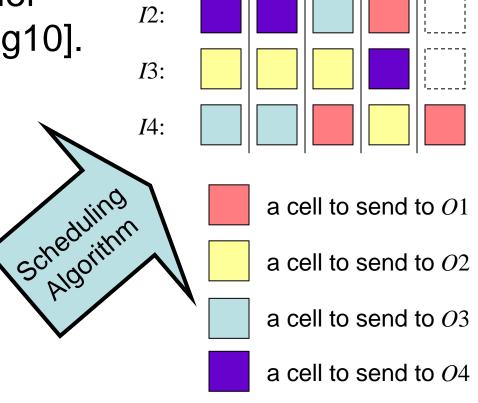
Cell time: 1

*I*1:

Theorem 1: If demand matrix' every color $\leq M$ cell, then have config. time scheduler with $O(N^4)$ time cost [wang10].

Demand

5



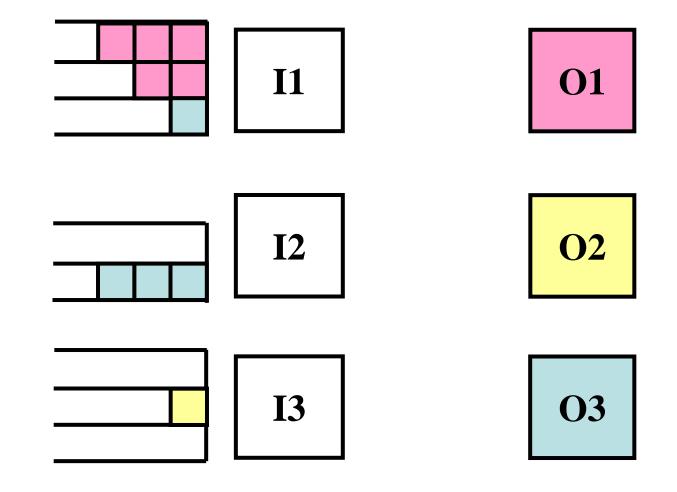
Schedule

3

5

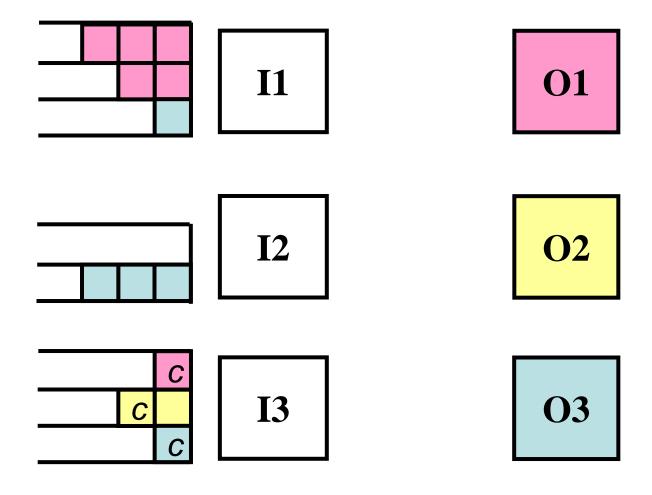


Support for Multicast





Support for Multicast





$$\vec{G}(V, \vec{E})$$

$$m = (s, D, w, T, H)$$

$$\mathcal{M} = \{m_i\}$$

$$q = (\vec{G}(V, \vec{E}), \mathcal{M})$$



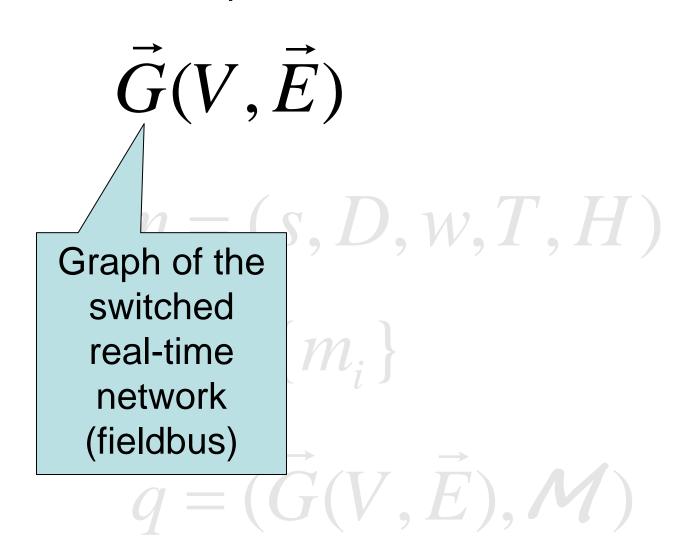
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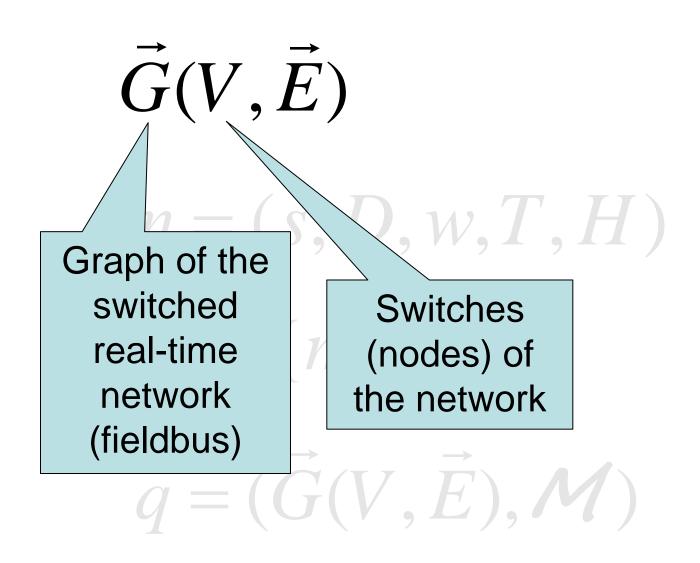
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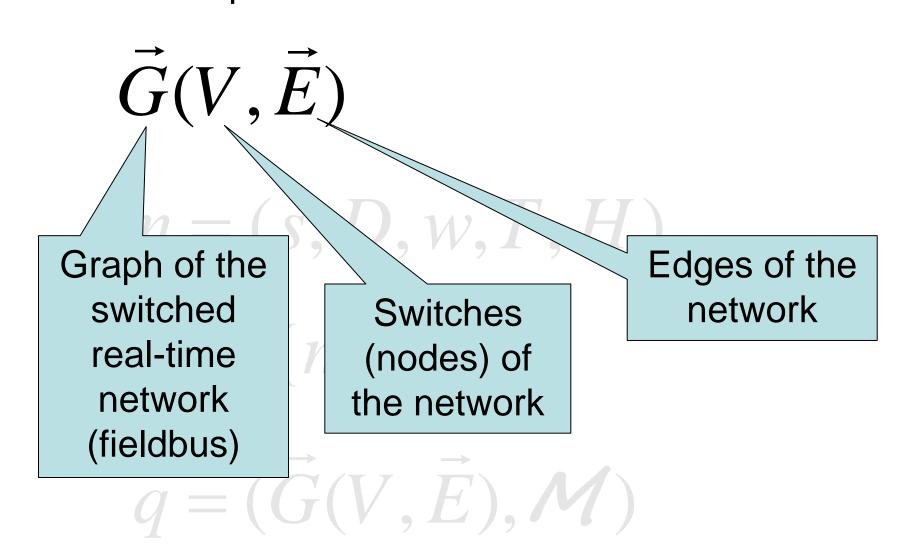














$$\vec{G}(V, \vec{E})$$

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$$\vec{G}(V, \vec{E})$$

$$m = (s, D, w, T, H)$$

$$M = \{m_i\}$$

A (real-time)
multicast group



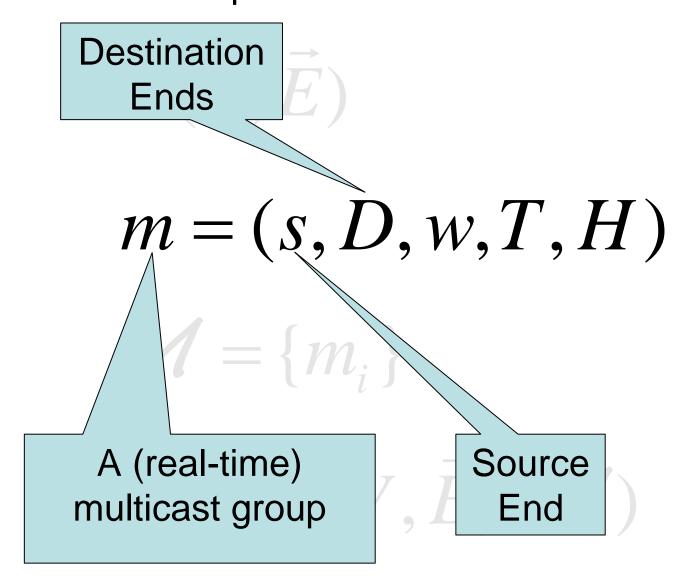
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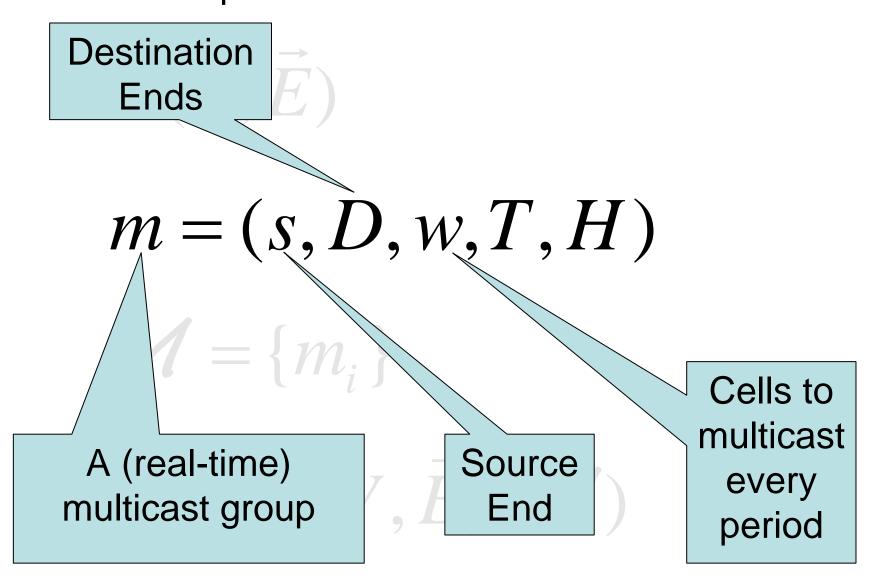
A (real-time)
multicast group

Source
End

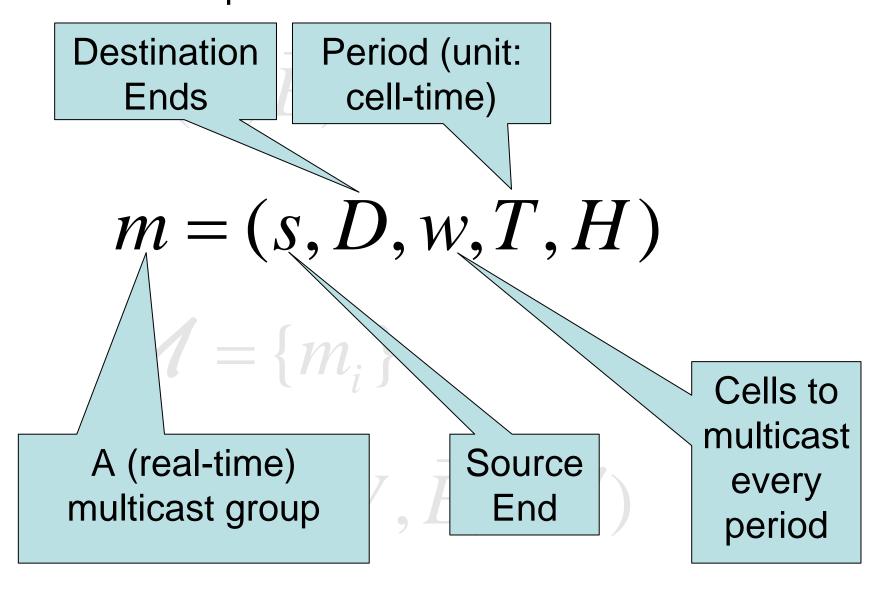














Destination Ends

Period (unit: cell-time)

Deadline (relative, unit: cell-time)

$$m = (s, D, w, T, H)$$

A (real-time) multicast group

Source End Cells to multicast every period



$$\vec{G}(V, \vec{E})$$

$$m = (s, D, w, T, H)$$

$$\mathcal{M} = \{m_i\}$$

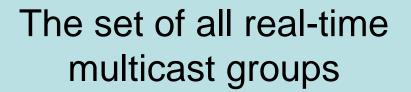
$$q = (\vec{G}(V, \vec{E}), M)$$



$$\mathcal{M} = \{m_i\}$$

$$q = (\vec{G}(V, \vec{E}), \mathcal{M})$$





The *i*th real-time multicast group

$$\mathcal{M} = \{ m_i \}$$

$$q = (\vec{G}(V, \vec{E}), \mathcal{M})$$



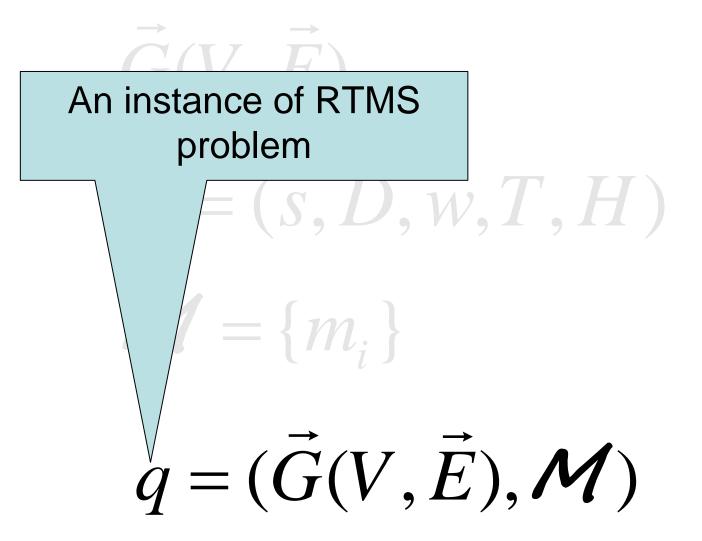
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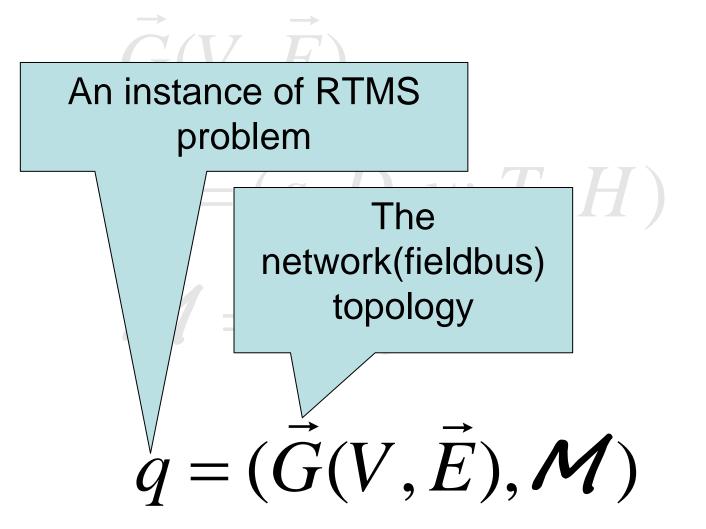
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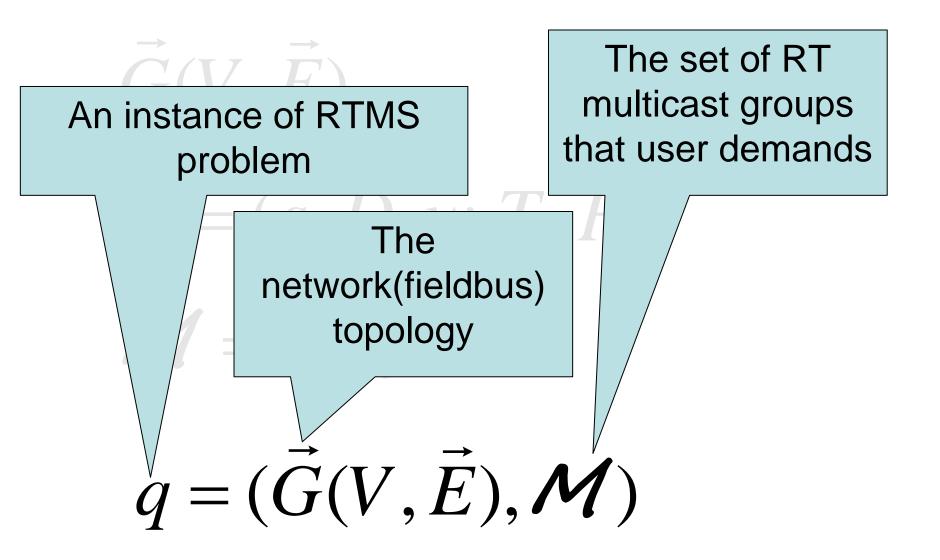














RTMS Problem: Given a q, how to schedule each switch s.t. every m_i meets needs?

$$\vec{G}(V, \vec{E})$$

$$m = (s, D, w, T, H)$$

$$\mathcal{M} = \{m_i\}$$

$$q = (\vec{G}(V, \vec{E}), \mathcal{M})$$



RTMS Problem: Given a q, how to schedule each switch s.t. every m_i meets its needs?

Theorem 2: RTMS Problem is NP-Hard.

M-slot Periodic RTMS: a subset of RTMS problems.

$$Q = \{q \mid q \text{ is an RTMS instance}\}$$

$$\begin{aligned} \mathbf{Q}' &= \{q'|\ q' = (\vec{G}, \mathbf{M}) \in \mathbf{Q}, \\ \mathbf{M} &= \{m_i\}, m_i = (s_i, D_i, w_i, T_i, H_i), \\ \text{and } \forall i, T_i \equiv M \} \end{aligned}$$



M-slot Periodic RTMS: a subset of RTMS problems.

Proposition 1: M-slot Periodic RTMS is NP-Hard.

 $\mathcal{M} = \{m_i\}, m_i = (s_i, D_i, w_i, T_i, H_i),$ and $\forall i, T_i \equiv M\}$



M-slot Periodic RTMS: a subset of RTMS problems.

Proposition 1: M-slot Periodic RTMS is NP-Hard.

Search for Heuristic Solutions.



Transform an M-slot Periodic RTMS instance into a Real-Time Multicast Routing (RTMR) instance.

Given

$$q' = (\vec{G}, \mathcal{M}) \in \mathcal{Q}',$$

where $\mathcal{M} = \{m_i\} = \{(s_i, D_i, w_i, T_i (\equiv M), H_i)\}, \text{ define }$

$$\tilde{q} = (\vec{G}, \tilde{\mathcal{M}}),$$

where $\widetilde{\mathcal{M}} = \{\widetilde{m}_i\} = \{(s_i, D_i, w_i, T_i (\equiv M), \widetilde{H}_i)\}$, and $\widetilde{H}_i = \max \left\{ \left| \frac{H_i - M}{M + 1} \right|, 0 \right\}.$



Transform an M-slot Periodic RTMS instance into a Real-Time Multicast Routing (RTMR) instance.

Given

M-slot Periodic RTMS instance

$$q' = (\vec{G}, \mathcal{M}) \in \mathcal{Q}',$$

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M-slot Periodic RTMS instance

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RTMR instance
$$\sim \tilde{q} = (\vec{G}, \tilde{\mathcal{M}}),$$

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Transform an M-slot Periodic RTMS instance into a Real-Time Multicast Routing (RTMR) instance.

M-slot Periodic RTMS instance

$$q' = (\vec{G}, \mathcal{M}) \in \mathcal{Q}',$$

where
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RTMR instance $= \widetilde{q} = (\vec{G}, \widetilde{\mathcal{M}}),$

$$\widetilde{q} = (\vec{G}, \widetilde{\mathcal{M}}),$$

Max Multicast Tree Height

where
$$\widetilde{\mathcal{M}} = {\{\widetilde{m}_i\}} = {\{(s_i, D_i, w_i, T_i (\equiv M), \widetilde{H}_i)\}}$$
, and

$$\widetilde{H}_i = \max \left\{ \left| \frac{H_i - M}{M + 1} \right|, 0 \right\}.$$



Transform an M-slot Periodic RTMS instance into a Real-Time Multicast Routing (RTMR) instance.

Given

A solution to
$$\tilde{q} = (\vec{G}, \vec{M})$$
 is

where
$$\mathcal{M} = \{m_i\} = \{(s_i, D_i, w_i, T_i (\equiv M), H \rightarrow \}, \text{ define}$$

a solution to $q' = (G, \mathcal{M})$.
 $\tilde{q} = (G, \tilde{\mathcal{M}}),$

where
$$\tilde{\mathcal{M}}=\{\tilde{m}_i\}=\{(s_i,D_i,w_i,T_i(\equiv M),\tilde{H}_i)\}$$
, and
$$\tilde{H}_i=\max\left\{\left|\frac{H_i-M}{M+1}\right|,0\right\}.$$



Transform an M-slot Periodic RTMS instance into a Real-Time Multicast Routing (RTMR) instance.

Giver

A solution to
$$\tilde{q} = (\vec{G}, \tilde{M})$$
 is

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a solution to $q' = (G, \mathcal{M})$.

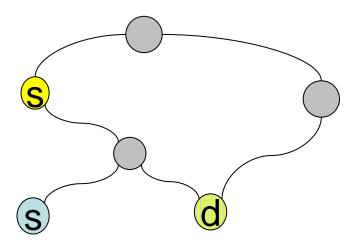
 $\tilde{q} = (\tilde{G}, M),$

RTMScheduling problem where $M = \{\tilde{m}_i\} = \{(s_i, D_i, H_i), H_i\}$, and becomes a Routing problem.



Existing mainstream internet multicast routing algorithms become Dijkstra when network is static and global info is available

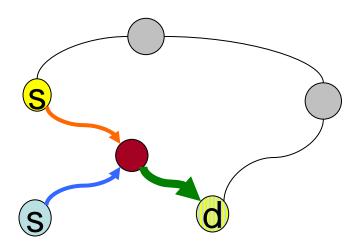
Dijkstra's short-coming: only cares about # of hops, ignores congestion.





Existing mainstream internet multicast routing algorithms become Dijkstra when network is static and global info is available

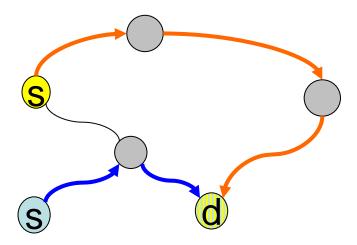
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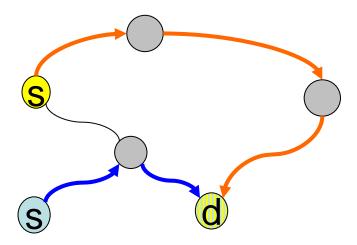
We want a heuristic routing algorithm that considers both (hops and congestion).





Existing mainstream internet multicast routing algorithms become Dijkstra when network is static and global info is available

We want a heuristic routing algorithm that considers both (hops and congestion).



Grow the multiple trees simultaneously with multiple iterations.

In each iteration, ≤1 link is added to each tree.

When multiple tree contends in a same switch, we carry out a job-hunting-like negotiation to let only ≤1 contending tree grow through an output in this iteration.





I1



different colors for different trees



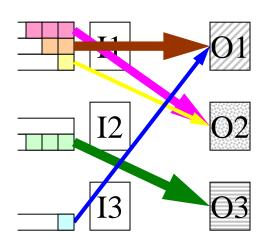
I2



___ I





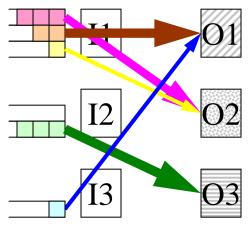


Each tree ranks all outputs and only apply to its favorite output

different colors for different trees







different colors for different trees

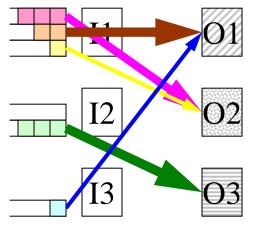
Each tree ranks all outputs and only apply to its favorite output



I1 01 02 12 02 13 03

Each output offers job to the most loyal applicant

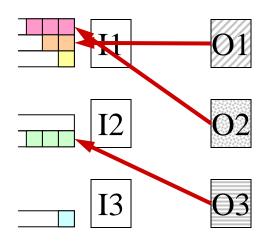




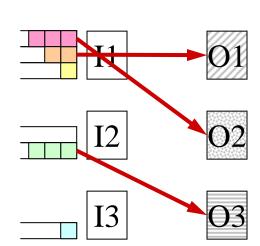
Each tree ranks all outputs and only apply to its favorite output



different colors for different trees



Each output offers job to the most loyal applicant



(1) (1) (1) (1) (1)

demand

matrix

Accept job by reserving corresponding frame slots.



$$r_{t,o} = \frac{\gamma_o(\tilde{H} - H(t,v))}{\operatorname{dis}(v, t.target)}$$

$$\gamma_o = \begin{cases} 1 & (\text{if } \max_{j \in \mathcal{O}_u} \{N_j\}) \\ = \max_{j \in \mathcal{O}_u} \{N'_j\}), \\ \exp(\max_{j \in \mathcal{O}_u} \{N_j\}) & (\text{otherwise}) \\ -\max_{j \in \mathcal{O}_u} \{N'_j\}) \end{cases}$$

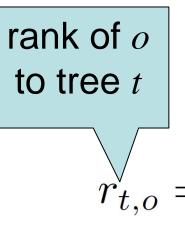


rank of *o* to tree *t*

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routing flexibility: slack to reaching max hop (max e2e delay) bound

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rank of o to tree t

routing flexibility: slack to reaching max hop (max e2e delay) bound

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 shortest distance to target end

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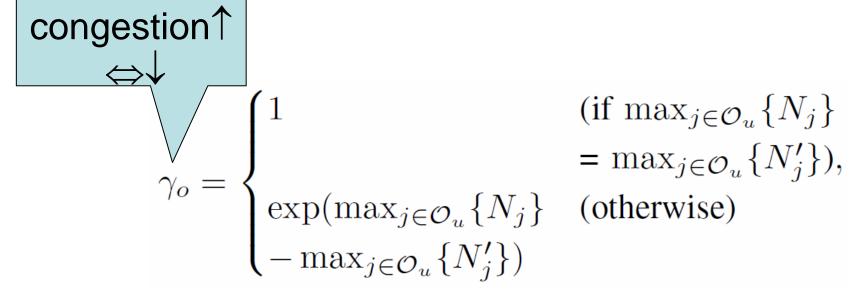


rank of *o* to tree *t*

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$$r_{t,o} = \frac{\gamma_o(\tilde{H} - H(t,v))}{\operatorname{dis}(v, t.target)}$$

shortest distance to target end



Definition of "favorite", a.k.a., "loyalty".

$$r_{t,o} = \frac{\gamma_o(\tilde{H} - H(t,v))}{\operatorname{dis}(v, t.target)}$$

$$o^{(t,1)} \stackrel{def}{=} \operatorname{argmax}_{o \in \mathcal{O}} \{r_{t,o}\}$$

$$o^{(t,2)} \stackrel{def}{=} \operatorname{argmax}_{o \in \mathcal{O} - \{o^{(t,1)}\}} \{r_{t,o}\}$$

t 's loyalty to $o^{(t,1)}$

$$r_{t,o^{(t,1)}} - r_{t,o^{(t,2)}}$$

4x4 port real-time switches

15x15 square grid network topology

Per port capacity: 1Gbps,

M = 2000 (cell/frame), 1 cell = 500 bit

10000 Trials, in each trial:

Random number of multicast groups,

 $w_i = 1~20 \text{ cell/frame } (500 \text{K}~10 \text{Mbps})$

4x4 port real-time switches

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Evaluation Setup.

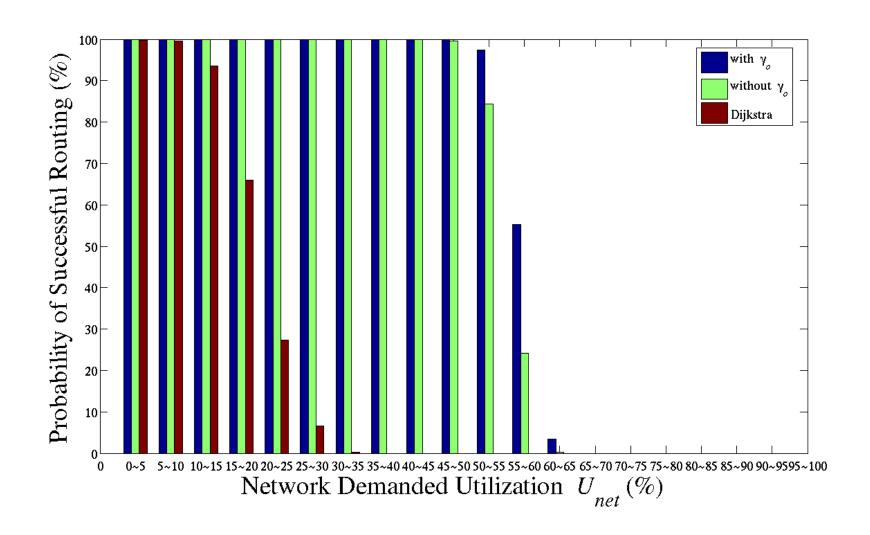
$$\tilde{H}_i = \eta H_i$$

Network Demanded Utilization (Application Layer E2E Utilization)

$$U_{net} \stackrel{def}{=} \frac{\sum_{i} (|D_i| w_i)}{|\bigcup_{i} \{D_i\}| M}$$

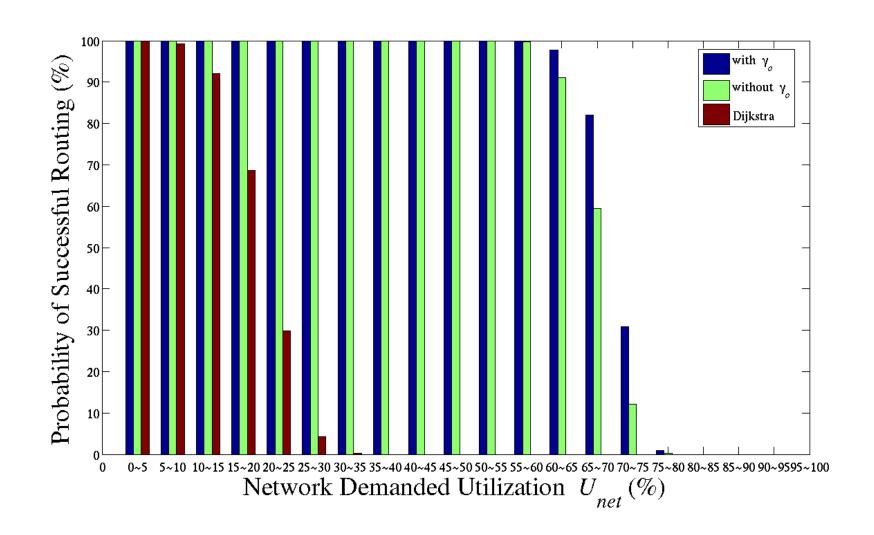


Evaluation Results: η=3





Evaluation Results: η=9





Mainstream Internet multicast routing algorithms mainly concern about dynamic distributed group management.

Reverse Path Broadcasting/Multicasting (RPB/RPM) [semeria97]

Truncated Reverse Path Broadcasting (TRPB) [semeria97]

Distance Vector Multicast Routing Protocol (DVMRP) [waitzman88]

Multicast Extension to Open Shortest Path First (MOSPF) [moy94a][moy94b]

Protocol Independent Multicast (PIM) [fenner06][adams05]

Core-Based Tree Multicast Routing (CBT) [ballardie97]



Mainstream Internet multicast routing algorithms become Dijkstra for static network with global info.

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Protocol Independent Multicast (PIM) [fenner06][adams05]

Core-Based Tree Multicast Routing (CBT) [ballardie97]



P2P and Overlay Network Multicast are concerned with statistical performance instead of hard real-time E2E delay bound.

Thank You!

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