# Improvement of Color Video Demosaicking in Temporal Domain

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Abstract—Color demosaicking is critical to the image quality of digital still and video cameras that use a single-sensor array. Limited by the mosaic sampling pattern of the color filter array (CFA), color artifacts may occur in a demosaicked image in areas of high-frequency and/or sharp color transition structures. However, a color digital video camera captures a sequence of mosaic images and the temporal dimension of the color signals provides a rich source of information about the scene via camera and object motions. This paper proposes an inter-frame demosaicking approach to take advantage of all three forms of pixel correlations: spatial, spectral, and temporal. By motion estimation and statistical data fusion between adjacent mosaic frames, the new approach can remove much of the color artifacts that survive intra-frame demosaicking and also improve tone reproduction accuracy. Empirical results show that the proposed inter-frame demosaicking approach consistently outperforms its intra-frame counterparts both in peak signal-to-noise measure and subjective visual quality.

*Index Terms*—Bayer color filter array, data fusion, digital video, subpixel motion estimation, temporal color demosaicking.

# I. INTRODUCTION

**M**OST digital cameras capture a color image with a single sensor array that sub-samples color bands in a particular mosaic pattern, such as the Bayer color filter array (CFA) [3] shown in Fig. 1. At each pixel, only one of the three primary colors (red, green, and blue) is sampled. The full color image is reconstructed by interpolating the missing color samples. This process is called color demosaicking, which is critical to the quality of reconstructed color images. The problem of color demosaicking has been extensively studied in spatial and frequency domains for still digital cameras [1], [2], [4], [6], [7], [9], [11], [13]–[17], [22], [23], [26]. Early demosaicking techniques mostly work in the spatial domain, such as nearest neighbor replication, bilinear interpolation, and cubic B-spline interpolation [13]. They are easy to implement but susceptible to many artifacts such as blocking, blurring and zipper effect at edges. The problem can be mitigated by an appropriate use

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Fig. 1. Bayer pattern.

of strong spectral correlation that exists in most natural color images. Indeed, most modern demosaicking methods exploit the correlation between red, blue, and green channels [2], [4], [6], [7], [9], [11], [13]–[17], [22], [23], [26]. To distinguish the existing methodology from the one of temporal demosaicking, we classify all the above color demosaicking techniques, either purely spatial or spatio-spectral methods, into the class of intra-frame demosaicking.

Even the sophisticated spatio-spectral color demosaicking techniques, such as those recently published, can still fail to faithfully reproduce the color components in the presence of high-frequency and/or sharp color transition structures. In order to surpass the current state-of-the-art in terms of image quality, additional information and constraints of the original color signals have to be brought into the demosaicking process. For digital video cameras, the temporal dimension of a sequence of mosaic frames captures more and new data on the scene, which would be otherwise absent if only a single frame is sampled by the CFA. A natural enquiry of practical significance is how to best exploit the correlation between adjacent frames and improve the accuracy and robustness of intra-frame color demosaicking.

Somewhat surprisingly, there seems to be little research reported on temporal color demosaicking, despite its obvious potential. Recently, Wu *et al.* proposed a joint spatial-temporal color demosaicking technique [24], [25]. Their main idea is to match the CFA green sample blocks in adjacent frames in such a way that the missing red and blue samples in one frame can be inferred from available red and blue samples of a matched adjacent frame. This technique is effective if the motion between the frames is by certain integer offsets that happen to align an available blue/red sample in one frame with a missing blue/red sample in the other frame. Another weakness of the technique is that it selects only one best reference sample from the adjacent frames and then fuses it with a spatially interpolated value.



Fig. 2. Flowchart of the proposed temporal demosaicking scheme.

In this paper, we propose a new framework of temporal color demosaicking to overcome these limitations. The progress is made in making multiple estimates of a missing color sample temporally and spatially from several reference frames. These estimates are first derived by associating samples of different frames via subpixel motion vectors, and then optimally fused into a single estimate of the missing color value.

For clarity of presentation and without the loss of generality, our discussions and algorithm development are around the ubiquitous Bayer CFA (see Fig. 1), which is used in most digital video cameras. The temporal demosaicking technique to be developed can be readily generalized to other CFA patterns. Note that the sampling frequency of the green channel is twice that of the red or blue channel in the Bayer pattern. This is because the sensitivity of human visual system peaks at the green wavelength and the green channel contributes the most to the luminance of an image. Since the red and blue channels are more sparsely sampled, we naturally anchor their reconstruction on the green channel in temporal demosaicking.

Fig. 2 is a schematic description of the proposed spatial-temporal demosaicking framework. First, the green channels of all frames are demosaicked individually by intra-frame demosaicking. Because the sampling frequency of green channel is twice that of red or blue channel in the Bayer pattern, the motion estimation between adjacent frames for temporal color demosaicking is based on the reconstructed green channel sequence. This design is to feed the motion analysis with the best information. With the estimated motion vectors, adjacent frames are registered spatially. The reference green samples in adjacent frames are then fused with the intra-frame estimates of the missing green samples of the current frame to enhance the green channel. The temporally enhanced green channel is then used to reconstruct the red and blue channels, by interpolating the missing red and blue samples using both the intra-frame and inter-frame information. First, individual red and blue frames are interpolated spatially using the correlation with corresponding green frames that have by now been demosaicked temporally. Then, the resulting spatio-spectrally demosaicked red and blue frames are enhanced temporally, guided by the motion vectors, by being fused with adjacent red and blue frames.

This paper is structured as follows. Section II introduces a new gradient-based intra-frame demosaicking method for the green channel by optimally weighting the horizontal and vertical interpolation results. The resulting green frames are used to compute the relative motions of adjacent frames in subpixel precision, which is the subject of Section III. After the frame registration, in Section IV, the reference frames are fused optimally with the current frame to obtain more robust estimates of the missing color samples. Section V presents the experimental results and Section VI concludes.

# II. GRADIENT-BASED INTRA-FRAME DEMOSAICKING OF THE GREEN CHANNEL

Since human visual systems are sensitive to the edge structures in an image, all adaptive demosaicking methods strive to avoid interpolating across edges. To this end, the gradient is estimated at each pixel, and the color interpolation is carried out directionally based on the estimated gradient. Directional filtering is the most popular approach to color demosaicking. A well-known directional interpolation scheme is the second order Laplacian correction proposed by Hamilton and Adams [7]. They used the second-order gradients of blue and red samples and the first-order gradient of green samples to interpolate the green channel. The red and blue samples are interpolated similarly with the correction of the second order gradients of the green samples. In this section, we propose a new intra-frame demosaicking method. The goal is to provide a good base for the next step of temporal demosaicking at a reasonable computational cost.

For ease of presentation and without loss of generality, we examine the case depicted by Fig. 3: a column and a row of alternating green and red samples intersect at a red sampling position where the missing green value needs to be estimated. The symmetric case of estimating the missing green values at the blue sampling positions of the Bayer pattern can be handled in the same way. Denote the red sample at the center of the window by  $R_0$ . Its interlaced red and green neighbors in horizontal direction are labeled as  $R_i^h$ ,  $i \in \{-2, 2\}$ , and  $G_i^h$ ,  $i \in \{-1, 1\}$ , respectively; similarly, the red and green neighbors of  $R_0$  in vertical direction are  $R_i^v$ ,  $j \in \{-2, 2\}$ , and  $G_i^v$ ,  $j \in \{-1, 1\}$ .

Most intra-frame demosaicking methods are based on an assumption that the difference between the green channel and the red/blue channel is a low-pass signal. Let  $\Delta_0 = G_0 - R_0$  be the unknown difference between green and red channels at the

| Image   | 1       | 2       | 3       | 4      | 5       | 6       | 7       | 8      |
|---------|---------|---------|---------|--------|---------|---------|---------|--------|
| $m_h$   | 0.0027  | 0.0013  | 0.0019  | 0.0004 | -0.0002 | -0.0005 | 0.0001  | 0.0018 |
| $m_{v}$ | -0.0007 | -0.0009 | -0.0014 | 0.0002 | -0.0013 | -0.0032 | -0.0005 | 0.0030 |
| С       | 0.0326  | 0.0927  | -0.0539 | 0.0696 | -0.0042 | 0.0281  | 0.0852  | 0.1592 |
| Image   | 9       | 10      | 11      | 12     | 13      | 14      | 15      | 16     |
| $m_h$   | -0.0027 | -0.0006 | -0.0000 | 0.0000 | 0.0008  | 0.0002  | 0.0001  | 0.0003 |
| $m_{v}$ | 0.0013  | -0.0006 | 0.0009  | 0.0028 | 0.0003  | -0.0004 | -0.0015 | 0.0006 |
| С       | -0.0011 | -0.0021 | 0.0176  | 0.0579 | 0.0597  | 0.1320  | 0.0575  | 0.0724 |

 TABLE I

 Means of  $v_0^h$  and  $v_0^v$  and Their Correlation Coefficients for the 16 Test Images in Fig. 4



of  $\Delta_0^h$  and  $\Delta_0^v$ . Denote by  $m_h$  and  $m_v$  the means of  $v_0^h$  and  $v_0^v$ and by c the correlation coefficient between  $v_0^h$  and  $v_0^v$ . Table I lists the values of  $m_h$ ,  $m_v$  and c for the 16 test images in Fig. 4, indicating that  $v_0^h$  and  $v_0^v$  are zero mean and nearly uncorrelated. These properties allow us to derive the optimal weights

where measurement noises  $v_0^h$  and  $v_0^v$  are the estimation errors

$$w_h = \frac{\sigma_v^2}{\sigma_h^2 + \sigma_v^2}, \quad w_v = \frac{\sigma_h^2}{\sigma_h^2 + \sigma_v^2} \tag{2-6}$$

Fig. 3. Row and column of mosaic data that intersect at a red sampling position.

sample position of  $R_0$ . The idea is to obtain an estimate of  $\Delta_0$ , denoted by  $\hat{\Delta}_0$ , and then recover the missing green sample by

$$G_0 \approx R_0 + \hat{\Delta}_0. \tag{2-1}$$

The reason for estimating the color difference signal  $\Delta = G - R$  rather than the green signal G directly is that  $\Delta$  is much smoother than G. Referring to Fig. 3, the horizontal and vertical differences between the green and red channels at  $R_0$  can be estimated as

$$\Delta_0^h = \frac{1}{2} \left( \mathbf{G}_{-1}^h + \mathbf{G}_1^h \right) - \frac{1}{4} \left( 2 \cdot \mathbf{R}_0 + \mathbf{R}_{-2}^h + \mathbf{R}_2^h \right) \quad (2-2)$$

$$\Delta_0^v = \frac{1}{2} \left( \mathbf{G}_{-1}^v + \mathbf{G}_1^v \right) - \frac{1}{4} \left( 2 \cdot \mathbf{R}_0 + \mathbf{R}_{-2}^v + \mathbf{R}_2^v \right).$$
(2-3)

In [7], the authors set  $\hat{\Delta}_0 = \Delta_0^h$  or  $\hat{\Delta}_0 = \Delta_0^v$  depending on which of the horizontal and vertical gradients is smaller, but this binary decision discards a potentially useful estimate. Instead, we can fuse the two estimates to obtain a more robust estimate of  $\Delta_0$ 

$$\hat{\Delta}_0 = w_h \Delta_0^h + w_v \Delta_0^v \tag{2-4}$$

where  $w_h + w_v = 1$ .

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Next, we discuss the determination of the weights  $w_h$  and  $w_v$ . Consider  $\Delta_0^h$  and  $\Delta_0^v$  as two independent measurements of the true color difference signal  $\Delta_0$ 

$$\Delta_0^h = \Delta_0 + v_0^h \text{ and } \Delta_0^v = \Delta_0 + v_0^v \tag{2-5}$$

where  $\sigma_h^2 = Var(v_0^h)$  and  $\sigma_v^2 = Var(v_0^v)$ . Here, the optimality is in the sense of mean square error (MSE), i.e.,  $w_h$  and  $w_v$  of (2-6) minimize the MSE of estimate  $\hat{\Delta}_0$ .

Empirically, we identify two main influence factors on the estimation errors of  $\Delta_0^h$  and  $\Delta_0^v$ . The first one is the amplitude of  $\Delta_0$ . Most natural scenes consist of predominantly pastoral (unsaturated) colors such that the color difference signal  $\Delta = G - R$  (or  $\Delta = G - B$ ) is not only smooth but also small in amplitude. The large amplitude of  $\Delta_0$  is typically associated with the discontinuity of the color difference signal at the position of  $R_0$ , increasing the risk of large estimation errors. In other words, the amplitudes of  $\Delta_0^h$  and  $v_0^v$ . The second factor affecting  $v_0^h$  and  $v_0^v$  is the presence of the high-frequency component in the luminance signal. To account for this, we measure the gradient of the red channel at  $R_0$  by

$$d_0^h = \mathbf{R}_0 - \frac{\mathbf{R}_{-2}^h + \mathbf{R}_2^h}{2} \text{ and } d_0^v = \mathbf{R}_0 - \frac{\mathbf{R}_{-2}^v + \mathbf{R}_2^v}{2}.$$
 (2-7)

Also, we observe that the level of  $v_0^h$   $(v_0^v)$  is nearly linearly proportional to the magnitudes of  $\Delta_0^h$   $(\Delta_0^v)$  and  $d_0^h$   $(d_0^v)$ . Let  $\Lambda_h = |\Delta_0^h| + |d_0^h|$  and  $\Lambda_v = |\Delta_0^v| + |d_0^v|$ . Fig. 5 plots the curve of  $\sigma_h$   $(\sigma_v)$  versus  $\Lambda_h$   $(\Lambda_v)$  for the first image in Fig. 4. The curves for other images are similar. These curves suggest that  $\sigma_h$   $(\sigma_v)$  is approximately proportional to  $\Lambda_h$   $(\Lambda_v)$ 

$$\sigma_h \approx \lambda_h \cdot \Lambda_h, \quad \sigma_v \approx \lambda_v \cdot \Lambda_v$$
 (2-8)



Fig. 5. Curves of  $\sigma_h$  versus  $\Lambda_h$  and  $\sigma_v$  versus  $\Lambda_v$ .

where  $\lambda_h$  and  $\lambda_v$  are constants, and  $\lambda_h \approx \lambda_v$  (see Fig. 5). Substituting (2-8) into (2-6) yields weights  $w_h$  and  $w_v$ , the final estimate  $\hat{\Delta}_0$  is more robust in reconstructing the missing green sample as  $G_0 = R_0 + \hat{\Delta}_0$ .

$$w_h = \frac{\Lambda_v^2}{\Lambda_h^2 + \Lambda_v^2}, \quad w_v = \frac{\Lambda_h^2}{\Lambda_h^2 + \Lambda_v^2}.$$
 (2-9)

Obviously, if  $\Delta_0^h$  and  $d_0^h$  have large magnitude, then  $w_h$  is small, reducing the influence of  $\Delta_0^h$  on  $\hat{\Delta}_0$ , and vice versa. By fusing the two directional estimates  $\Delta_0^h$  and  $\Delta_0^v$  with optimal

# III. MOTION ESTIMATION AND RE-SAMPLING

Upon spatially demosaicking the green channel of each frame, we take the next step of temporal demosaicking to enhance the green channel by exploiting the temporal correlation of the video signal. The promise of temporal color demosaicking lies in the fact that the color samples missed by



Fig. 6. Current green frame and its backward and forward neighboring frames.

the CFA subsampling process in one frame may be captured in neighboring frames. To realize this potential, we have to register the frames by determining the relative motion vectors between the current frame and the reference frames. Accurate motion estimation of the video frames is pivotal to temporal color demosaicking and many applications such as video coding, superresolution imaging, and computer vision [5], [8], [12], [18]–[21].

In the Bayer CFA, the green channel has twice as many samples as the red and blue channels. Furthermore, the green signal is a good approximation of the luminance signal. For these reasons, we estimate the motions in the green channel. This is also why an initial intra-frame demosaicking process is required to estimate the missing green samples prior to temporal demosaicking.

Any of the existing motion-estimation techniques can be used to estimate the motion vector in the green channel. A more accurate motion estimation method may lead to a better temporal demosaicking result, but of course at a higher computational cost. It should be stressed, however, that the temporal enhancement technique to be developed in the next section is independent of the motion estimation method. The main focus of this paper is on the methodology of temporal enhancement rather than motion estimation. For a good balance between estimation accuracy and low complexity, we choose the block-based motion-estimation technique, which is widely used in MPEG 2/4 and other video-coding standards [12]. Specifically, we adopt the cross-correlation-based method proposed in [27] to compute the motion vector in subpixel precision. For the sake of continuity, we briefly describe the method below.

As the convention of this paper, we denote the original green samples by G and the interpolated green samples through the intra-frame demosaicking by  $\hat{G}$  (referring to Fig. 6). Let M be a block of pixels in the current frame and  $M_{i,j}$  a matched block in a reference frame with displacement (i, j), where *i* and *j* are integers. Denote by  $(\tau_x, \tau_y)$  the real valued motion vector of M from the current frame to the reference frame.



Fig. 7. Re-sampling of the reference block.

For convenience, let M and  $M_{i,j}$  be the matrices whose elements are the sample values of blocks **M** and **M**<sub>i,j</sub>. The cross-correlation function between M and  $M_{i,j}$  is computed as

$$r(i,j) = \sum_{n=1}^{N_x} \sum_{m=1}^{N_y} M(n,m) M_{i,j}(n,m)$$
(3-1)

where the dimensions of M and  $M_{i,j}$  are  $N_x \times N_y$ . If the motion vector  $(\tau_x, \tau_y)$  is restricted to integer precision, then it can be approximated by

$$(\tau_x, \tau_y) \approx (i_0, j_0) = \arg \max_{i, j \in Z} r(i, j).$$
(3-2)

However, since the true displacement of a scene in two frames is in general subpixel, we should allow the motion vector  $(\tau_x, \tau_y)$  to be real valued for higher precision.

Consider the motion in the horizontal and vertical directions separately. For a fixed y, we write the continuous cross-correlation function r(x, y) as  $r_x(x)$ . In [27], we showed that the one-dimensional cross correlation function can be well approximated by a Gaussian function in the interval around its peak, for digital signals that are captured by sensors whose kernel function is Gaussian or box. Therefore, we write r(x, y) in the horizontal direction as

$$r_x(x) = a \cdot e^{-b(x-c)^2}$$
 (3-3)

and use the three most significant samples in horizontal direction  $r(i_0, j_0), r(i_0, j_0-1)$ , and  $r(i_0, j_0+1)$  to fit  $r_x(x)$  and solve for the three parameters a, b, and c. Letting  $r(i_0, j_0) = r_x(0)$ ,  $r(i_0, j_0 - 1) = r_x(-1)$ , and  $r(i_0, j_0 + 1) = r_x(1)$ , we have

$$\begin{cases} \ln r(i_0, j_0 - 1) = \ln a - b(1 + c)^2 \\ \ln r(i_0, j_0) = \ln a - bc^2 \\ \ln r(i_0, j_0 + 1) = \ln a - b(1 - c)^2. \end{cases}$$
(3-4)

Solving (3-4) yields

$$c = \frac{r(i_0, j_0 + 1) - r(i_0, j_0 - 1)}{4r(i_0, j_0) - 2r(i_0, j_0 - 1) - r(i_0, j_0 + 1)}.$$
 (3-5)



Fig. 8. (a) Interpolation of a missing red sample at a green pixel whose horizontal neighbors are red pixels. (b) Interpolation of a missing red sample at a green pixel whose vertical neighbors are red pixels. (c) Interpolation of a missing red sample at a blue pixel.

The motion value  $\tau_x$  in the horizontal direction is determined to be the peak position of  $r_x(x)$ , i.e.,  $\tau_x$  is the sum of integral part  $j_0$  and fractional part c solved in (3-5)

$$\tau_x = j_0 + c. \tag{3-6}$$

Similarly, we can compute  $\tau_y$ , the motion in vertical direction, and then determine the motion vector  $(\tau_x, \tau_y)$ .

Since  $(\tau_x, \tau_y)$  is real valued in subpixel precision, the corresponding reference block matched to  $\mathbf{M}$ , denoted by  $\mathbf{M}_c$ , should be re-sampled from the reference frame. In the literature the value of a pixel is commonly modeled as the integral of the light over a unit square. Let  $\mathbf{P}_c$  be a pixel in  $\mathbf{M}_c$  and suppose the pixel square of  $\mathbf{P}_c$  overlaps with those of  $\mathbf{P}_1$ ,  $\mathbf{P}_2$ ,  $\mathbf{P}_3$ , and  $\mathbf{P}_4$ , as shown in Fig. 7, which are the pixels in the reference frame.  $\mathbf{P}_c$  is to be reproduced from  $\mathbf{P}_1$ ,  $\mathbf{P}_2$ ,  $\mathbf{P}_3$ , and  $\mathbf{P}_4$ . Denote the areas of the overlaps as  $\mathbf{S}_1$ ,  $\mathbf{S}_2$ ,  $\mathbf{S}_3$ , and  $\mathbf{S}_4$ , which can be computed from the fractional part of the real valued coordinate  $(\tau_x, \tau_y)$ . Then the value of pixel  $\mathbf{P}_c$  can be calculated as the sum of the intensities over  $\mathbf{S}_1$ ,  $\mathbf{S}_2$ ,  $\mathbf{S}_3$ , and  $\mathbf{S}_4$ :  $\mathbf{P}_c = \sum_{i=1}^4 \mathbf{S}_i \cdot \mathbf{P}_i$ .

Due to the structure of the sampling grid of the green channel, two of the four squares  $P_1$ ,  $P_2$ ,  $P_3$ , and  $P_4$  are the original green samples G and the other two are the interpolated green samples  $\hat{G}$  (see Fig. 6). To factor in higher confidence on G than on  $\hat{G}$ , we put different confidence factors  $c_i$  on  $P_1$ ,  $P_2$ ,  $P_3$ , and  $P_4$ when computing  $P_c$ 

$$P_c = \sum_{i=1}^{4} c_i \cdot S_i \cdot P_i \tag{3-7}$$

where weight  $c_i = 1.2$  if  $P_i$  is an original green sample and  $c_i = 0.8$  if  $P_i$  is an interpolated green sample. The sum of weights should be  $\sum_{i=1}^{4} c_i = 4$ .

#### IV. TEMPORAL IMPROVEMENT OF DEMOSAICKING

Intra-frame spatial demosaicking has an inherent limitation. It is impossible to reconstruct faithfully the color signal at/near the edge/texture structures whose frequency exceeds the Nyquist sampling limit. To aggravate the problem, the human visual system is very sensitive to the color artifacts across edges. The demosaicking errors become visually highly objectionable if the



Fig. 9. (a) Resolution chart image. (b) Synthetic image that contains pure red, green, and blue color objects.

discontinuity exists simultaneously in luminance and chrominance. In this case, the artifacts cannot be removed by assuming a high correlation between the color channels as most intraframe demosaicking algorithms do. In contrast, temporal correlation of a mosaic color video signal, which commonly exists, provides badly needed information to resolve such difficult cases for color demosaicking.

### A. Temporal Update of Green Channel

With the motion estimation and re-sampling algorithms described in Section III, we can get a reference block of the current block  $\mathbf{M}_0$  in each reference frame. Suppose that Kreference frames are used, and denote by  $\{\mathbf{M}_i\}_{i=1,2,...,K}$  the re-sampled reference blocks. The spatially demosaicked sample in  $\mathbf{M}_0$  is to be fused with the matched samples in  $\mathbf{M}_i$ . For convenience of expression, we denote the spatially interpolated green sample in  $\mathbf{M}_0$  by  $\hat{\mathbf{G}}_0$ , the unknown true green sample corresponding to  $\hat{\mathbf{G}}_0$  by  $\mathbf{G}$ , and the associated reference samples in  $\mathbf{M}_i$  by  $\hat{\mathbf{G}}_i$ . Naturally, we can write  $\hat{\mathbf{G}}_0$  and  $\hat{\mathbf{G}}_i$  as the measurements of true sample  $\mathbf{G}$ 

$$\hat{\mathbf{G}}_i = \mathbf{G} + e_i, \quad i = 0, 1, \dots, K$$
 (4-1)

where  $e_i$  are the interpolation errors of  $\hat{G}_i$  in the spatial demosaicking process, and they are uncorrelated with G. Since  $\hat{G}_i$  are independent observations of G in different frames, we assume that errors  $e_i$ , i = 0, 1, ..., K, are mutually nearly uncorrelated. Indeed, the correlation coefficient between  $e_i$  and  $e_j$ ,  $i \neq j$ , is only 0.11 on average for the test sequences used in Section V. Furthermore, this correlation is much weaker in areas of edges and textures, where temporal demosaicking offers clear advantage over spatial demosaicking, than smooth areas. If  $e_i$ 's are significantly correlated, then the observations  $\hat{G}_i$  are very similar (e.g., if there is no acquisition noise and no motion,  $\hat{G}_i$  will be identical to each other). In this case, the reference frames offer very little new information and temporal demosaicking cannot improve spatial demosaicking.

In order to fuse all the measurements  $\hat{G}_i$  into a more robust estimate of G, we consider the weighted estimate

$$\overline{\mathbf{G}} = \sum_{i=0}^{K} w_i \hat{\mathbf{G}}_i \tag{4-2}$$

where weights  $\sum_{i=0}^{K} w_i = 1$ . The criterion of determining  $w_i$  is to minimize the MSE of  $\overline{G}$ , i.e.,  $\{w_i\} = \arg \max_{\sum_i w_i = 1} E[(\overline{G} - \sum_i w_i)]$ 

 $G)^2$ ], where E is the expectation operator.

The weights  $w_i$  may be determined off-line using an appropriate training set. The weights optimized for the training set can then be used in (4-2) to obtain the fused estimate  $\overline{G}$ . However, if the training dataset is not available, or/and if the best color demosaicking performance is desired, on-line adaptive estimation can be made as described below. Let

$$\Omega = E\left[(\overline{\mathbf{G}} - \mathbf{G})^2\right] = E\left[\left(\sum_{i=1}^K w_i e_i + \left(1 - \sum_{i=1}^K w_i\right) e_0\right)^2\right].$$
(4-3)

Denote by  $\sigma_i^2$  the variance of error  $e_i$ . Differentiating  $\Omega$  with respect to  $e_i$ , i = 1, 2, ..., K, and setting the partial derivatives to zero. With  $E[e_i e_j]|_{i \neq j} \approx 0$ , we have

$$\frac{\partial \Omega}{\partial w_i} = w_i \sigma_i^2 - \left(1 - \sum_{j=1}^K w_j\right) \sigma_0^2 = 0$$

from which we obtain the optimal weight vector  $\mathbf{w} = col\{w_1, w_2, \dots, w_K\}$  for the estimates in the K reference frames

$$\mathbf{w} = \mathbf{S}^{-1}\mathbf{1} \tag{4-4}$$

where 1 is a column vector whose elements are all ones and the  $K \times K$  matrix S is

$$\mathbf{S} = \begin{bmatrix} 1 + \sigma_1^2 / \sigma_0^2 & 1 & \cdots & 1 \\ 1 & 1 + \sigma_2^2 / \sigma_0^2 & \cdots & 1 \\ \vdots & \vdots & \ddots & \vdots \\ 1 & 1 & \cdots & 1 + \sigma_K^2 / \sigma_0^2 \end{bmatrix}.$$
 (4-5)



Fig. 10. (a) Original image; demosaicked images by the methods in (b) [7]; (c) [4]; (d) [9]; (e) [16]; (f) [15]; (g) [26]; (h) [24]; and (i) the proposed temporal scheme.

Solving (4-4) for  $w_i$ , the fused estimate of G is then computed by (4-2).

| Domoscioling Mothoda     | Simula | Simulated sequence 1 |       |       | Simulated sequence 2 |       |  |  |
|--------------------------|--------|----------------------|-------|-------|----------------------|-------|--|--|
| Demosaicking Methous     | red    | green                | blue  | Red   | green                | blue  |  |  |
| Method in [7]            | 23.98  | 30.54                | 23.95 | 23.99 | 36.83                | 23.43 |  |  |
| Method in [4]            | 17.95  | 27.95                | 17.99 | 8.06  | 8.00                 | 7.90  |  |  |
| Method in [9]            | 29.82  | 31.78                | 29.94 | 22.66 | 33.91                | 22.40 |  |  |
| Method in [16]           | 24.71  | 28.69                | 24.76 | 22.43 | 28.58                | 23.99 |  |  |
| Method in [15]           | 30.17  | 33.49                | 30.21 | 24.26 | 37.00                | 23.63 |  |  |
| Method in [26]           | 34.84  | 36.41                | 34.53 | 22.55 | 35.45                | 21.96 |  |  |
| Method in [24]           | 32.85  | 37.58                | 33.13 | 32.87 | 43.58                | 31.78 |  |  |
| Proposed temporal method | 35.76  | 40.38                | 35.77 | 33.69 | 46.20                | 32.60 |  |  |

 TABLE II

 PSNR (dB) Results on the Two Synthetic Sequences by Different Methods

#### B. Estimation of the Error Variances

To implement the above algorithm, the error variances  $\sigma_i^2$  need to be estimated. From  $\hat{\mathbf{G}}_i = \mathbf{G} + e_i$  and  $E[e_i e_j]|_{i \neq j} \approx 0$ , we have

$$d_{i,j} = E\left[ (\hat{G}_i - \hat{G}_j)^2 \right] \\ = \sigma_i^2 + \sigma_j^2, \quad i, j = 0, 1, \dots, K \text{ and } i \neq j.$$
(4-6)

The values of  $d_{i,j}$  can be estimated adaptively from blocks  $\mathbf{M}_i$ and  $\mathbf{M}_j, i \neq j$ 

$$d_{i,j} = \frac{1}{L} \sum_{\hat{\mathbf{G}}_i \in \mathbf{M}_i, \hat{\mathbf{G}}_j \in \mathbf{M}_j} (\hat{\mathbf{G}}_i - \hat{\mathbf{G}}_j)^2$$
(4-7)

where L is the total number of missing green samples in blocks  $M_i$ .

If  $\sigma_0^2$ , i.e., the variance of  $e_0$  in the current block  $\mathbf{M}_0$ , is a known prior, then the values of  $\sigma_i^2$  for other *i*'s can be calculated by (4-6) and (4-7). Otherwise, all the values of  $\sigma_i^2$  can be estimated as follows. Let

$$\boldsymbol{\sigma} = col\left\{\sigma_0^2, \dots, \sigma_K^2\right\} \tag{4-8}$$

be a  $K+1\mbox{-dimensional vector that encompass all the <math display="inline">\sigma_i^2,$  and let

$$\mathbf{d} = col\{d_{0,1}, \dots, d_{0,K}, d_{1,2}, \dots, d_{1,K}, \dots, d_{K-1,K}\}$$
(4-9)

be a K(K + 1)/2-dimensional vector that encompass all the  $d_{i,j}$ , then there exists a  $K(K + 1)/2 \times (K + 1)$  matrix **H** such that

$$\mathbf{d} = \mathbf{H}\boldsymbol{\sigma}.\tag{4-10}$$

Denote  $\mathbf{h}_{i,j}$  as the row in  $\mathbf{H}$  such that  $d_{i,j} = \mathbf{h}_{i,j}\boldsymbol{\sigma}$ . Clearly, only the  $i^{\text{th}}$  and  $j^{\text{th}}$  th elements in  $\mathbf{h}_{i,j}$  are 1 and all other elements are zeros. We estimate  $\boldsymbol{\sigma}$  by the least-square estimation technique

$$\boldsymbol{\sigma} = (\mathbf{H}'\mathbf{H})^{-1}\mathbf{H}'\mathbf{d}.$$
 (4-11)

## C. Joint Spatial-Temporal Interpolation of Red/Blue Channels

After the green estimates are improved by the temporal demosaicking process described in Sections IV-A and IV-B, they can in turn guide the demosaicking of the red and blue channels. Similarly to the demosaicking of the green channel, the missing red and blue samples are recovered in two steps. First, we spatially interpolate them with the help of the temporally demosaicked green channel and then temporally improve the interpolation results aided by motion vectors.

The intra-frame demosaicking of red/blue channel can be accomplished by any of the existing methods. In this paper, we adopt the directional filtering strategy similar to Hamilton and Adams' method [7]. Since the interpolation of blue channel is symmetrical to that of red channel, we only describe the process of interpolating the red channel.

Referring to Fig. 8, there are three cases depending on the positions of missing red samples. Fig. 8(a) and (b) shows the two cases of the missing red samples at the original green pixel positions. Fig. 8(c) shows the case of a missing red sample at the original blue pixel position. We stress the fact that the missing green samples at the red/blue positions have already been estimated. In the case of Fig. 8(a), we can estimate the green-red difference signal by using the true red samples and temporally estimated green samples in horizontal direction, and in the case of Fig. 8(b), we can estimate the green-red difference signal in vertical direction similarly. In the case of Fig. 8(c), we can estimate two green-red difference values in 45° and 135° directions. These two values are fused to one result as what we did in Section II. The missing red sample is estimated by subtracting the estimated green-red difference  $\hat{\Delta}$  from the original green value,  $\hat{R} = G - \hat{\Delta}$ , in cases (a) and (b), or from the estimated green value,  $\hat{\mathbf{R}} = \hat{\mathbf{G}} - \hat{\Delta}$ , in case (c). Since the above spatial



green channel, the spatial interpolation of red and blue channels indirectly benefits from the temporal redundancy in adjacent frames.

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Similarly to the green channel, the spatially interpolated red and blue channels can be further improved via motion estimation and data fusion. However, the motion vectors are still computed in the green channel, because the motion estimation accuracy in the green channel is much higher than in the red and blue channels. Indeed, the sample frequency of red/blue channel is only half of that of the green channel, and the two-dimensional (2-D) sampling grid of red/blue channel employs inefficient square lattice as opposed to the diamond lattice for the green channel.

The temporal enhancement process of red/blue channel is similar to that of green channel. The main difference is in the confidence factor determination in the re-sampling step. Take the red channel for example, after the motion vector  $(\tau_x, \tau_y)$ between a current block **M** and a reference block  $\mathbf{M}_c$  is computed, a pixel  $\mathbf{P}_c$  in  $\mathbf{M}_c$  needs to be re-sampled from the four neighboring pixels  $\mathbf{P}_1$ ,  $\mathbf{P}_2$ ,  $\mathbf{P}_3$ , and  $\mathbf{P}_4$  in the reference frame. In the sampling grid of the red channel, only one of the four pixels is an original red sample R and the other three are interpolated ones  $\hat{\mathbf{R}}$ . The confidence factors in the re-sampling process  $\mathbf{P}_c = \sum_{i=1}^4 c_i \cdot \mathbf{S}_i \cdot \mathbf{P}_i$  are  $c_i = 1.6$  if  $\mathbf{P}_i$  is an original red sample and  $c_i = 0.8$  if  $\mathbf{P}_i$  is an interpolated red sample. This is to guarantee that the sum of all  $c_i$  to be 4.

# V. EXPERIMENTAL RESULTS

The proposed joint spatial-temporal color demosaicking algorithm was implemented and tested on two synthetic sequences and two real video clips. To evaluate the performance of the proposed algorithm in comparison with other intra-frame demosaicking algorithms and our earlier temporal demosaicking algorithm [24], [25], we present in this section both the demosaicked images and PSNR results. Besides the temporal method in [24], the six state-of-the-art intra-frame demosaicking algorithms used in our comparison are: the method of second-order Laplacian filtering by Hamilton and Adams [7], the method of variable number of gradients by Chang *et al.* [4], the principal vector method by Kakarala and Baharav [9], the bilinear interpolation of color difference by Pei and Tam [16], the normalized color-ratio modeling by Lukac and Plataniotis [15], and the directional filtering and fusion method by Zhang and Wu [26].

#### A. Test on Synthetic Mosaic Video Sequences

1) Resolution Chart Video: To validate the proposed demosaicking algorithm, we used two synthetic mosaic test sequences. The first sequence is generated from a gray-scale resolution chart [Fig. 9(a)], which is widely used in evaluating superresolution algorithms. Denote by I the original resolution chart image. We simulated five mosaic video frames with relative motions as follows.

To simulate a video camera, I is first smoothed by convoluting with a low-pass filter  $f_s : I_s = I * f_s$ , where  $f_s = [1, 1, 1; 1, 8, 1; 1, 1, 1]/16$  in this experiment. Then five

Fig. 11. (a) Original image; demosaicked images by the methods in (b) [7]; (c) [4]; (d) [9]; (e) [16]; (f) [15]; (g) [26]; (h) [24]; and (i) the proposed temporal scheme.

demosaicking process exploits the spectral correlation between red/blue and green, and it operates on temporally demosaicked



Fig. 12. Scene in the (a) first test clip and (b) second test clip.

| Damosajaking Mathods     | Tes   | Test sequence 1 |       |       | Test sequence 2 |       |  |
|--------------------------|-------|-----------------|-------|-------|-----------------|-------|--|
| Demosaicking Methoas     | red   | green           | blue  | Red   | green           | blue  |  |
| Method in [7]            | 31.53 | 33.61           | 27.87 | 33.16 | 38.30           | 36.16 |  |
| Method in [4]            | 31.46 | 33.41           | 27.52 | 32.61 | 37.90           | 33.79 |  |
| Method in [9]            | 30.66 | 34.08           | 29.24 | 31.76 | 38.42           | 35.72 |  |
| Method in [16]           | 30.83 | 34.37           | 29.14 | 31.59 | 36.29           | 35.15 |  |
| Method in [15]           | 30.11 | 33.09           | 28.99 | 31.68 | 36.71           | 35.93 |  |
| Method in [26]           | 30.48 | 35.25           | 29.74 | 31.23 | 38.24           | 35.62 |  |
| Method in [24]           | 32.24 | 35.15           | 30.10 | 34.15 | 38.11           | 36.06 |  |
| Proposed temporal method | 34.42 | 36.10           | 30.57 | 36.62 | 38.87           | 37.85 |  |

 TABLE III

 PSNR (dB) Results on the Two Synthetic Sequences by Different Methods

frames are created by down-sampling  $I_s$ . The current frame to be enhanced is

$$F_0(n,m,\bullet) = I_s(2n,2m,\bullet)$$

where " $\bullet$ " is the index for color channels. The other four reference frames are

$$F_1(n, m, :) = I_s(2n, 2m + 2, \bullet) + v_1$$

$$F_2(n, m, \bullet) = I_s(2n + 2, 2m, \bullet) + v_2$$

$$F_3(n, m, \bullet) = I_s(2n + 2, 2m + 2, \bullet) + v_3$$

$$F_4(n, m, \bullet) = I_s(2n - 1, 2m + 1, \bullet) + v_4$$

where  $v_1, v_2, v_3$ , and  $v_4$  are Gaussian white noises and they are mutually uncorrelated. In our simulation,  $v_i \sim N(0, 8)$ , i = 1, 2, 3, 4. The relative motions between  $F_i$ , i = 1, 2, 3, 4 and  $F_0$ are (0, 1), (1, 0), (1, 1), and (-0.5, 0.5), respectively. Finally, each frame  $F_i$  is down-sampled again according to the Bayer pattern.

The demosaicked results of different methods for the resolution chart video are presented in Fig. 10, where (a) is the original, (b)–(g) show the demosaicked images by the intra-frame methods in [4], [7], [9], [15], [16], and [26]. These methods produce highly visible color artifacts. Fig. 10(h) and (i) shows the output images of a previous temporal demosaicking method [24] and the proposed method. One can see that only the new method is free of color artifacts on the resolution test sequence. The PSNR results are listed in Table II, which are in agreement with the visual quality evaluations. The proposed joint spatial-temporal method has the highest PSNR.

2) Saturated Color Video: The simulation results on the resolution chart demonstrate the effect of the joint spatial-temporal demosaicking approach on the high-frequency luminance contents. Now we turn to the other more difficult form of discontinuity for color demosaicking: abrupt chrominance changes. Fig. 9(b) represents such an artificial worst-case scenario: a scene consisting of sharp objects of highly saturated colors (pure red, green, and blue) in a white background. We generated a mosaic video sequence from Fig. 9(b) in the same way as described in the previous subsection. The demosaicked images of this test sequence are presented in Fig. 11. All the intra-frame methods generate highly visible color artifacts around the object boundaries. In contrast, the temporal demosaicking approach performs very well in reproducing the sharp color edges. The PSNR results are also listed in Table II.

The color artifacts caused by chrominance discontinuities (e.g., lack of spectral correlation in saturated colors) are more difficult to remove than those caused by luminance discontinuities within a frame. In this case, the common assumption made by almost all intra-frame demosaicking algorithms on the smoothness of the color difference signal no longer holds. As we see in this experiment and the following experiments, this problem can be mitigated by exploiting the temporal correlation.



Fig. 13. (a) Original image; demosaicked images by the methods in (b) [7]; (c) [4]; (d) [9]; (e) [16]; (f) [15]; (g) [26]; (h) [24]; and (i) the proposed temporal scheme.

# B. Experiments on Real Video Clips

A similar comparison study was also carried out on two real video clips. The movie sequences were originally captured on film and then digitized by a high-resolution scanner.<sup>1</sup> All the three color channels were known and we simulated the mosaic data by subsampling the red, green, blue channels according to the Bayer pattern. In temporal demosaicking of a current frame, we used two immediately proceeding frames and two immediately succeeding frames as reference frames.

The scene in the first movie clip is a car in a park. The car is still but the camera is rotating around it. Fig. 12(a) shows the scene in a frame. The video is captured at a rate of 24-frames/second. The spatial resolution of each frame is 1948  $\times$  1280 and the bit depth is 8 bits per color channel. In this clip, most of the smooth background objects such as the road, the lake, and trees can be reconstructed free of visible artifacts by spatial demosaicking techniques. However, on the car, where some sharp edges accompany abrupt color changes, the spatial demosaicking cannot faithfully recover the missing color components. Fig. 13(a) shows a 256  $\times$  256 portion of the original frame in question.

Fig. 13(b)-(i) shows the demosaicked images by the eight methods. Fig. 14(a)-(i) presents the close-ups of the demosaicked images by these methods for easier visual inspection. There are highly visible color artifacts in Fig. 13(b)–(g), particularly on the grill of the car, where the true color signal frequency exceeds the sampling frequency of the Bayer CFA. The algorithm in [26] [see Fig. 13(g)] has fewer color artifacts on the grill than other intra-frame demosaicking methods, but it still generates significant zipper effects along the boundary of the red and silver colors and on the emblem of the car [see Fig. 14(g)], as other spatial demosaicking methods [see Fig. 14(b)-(f)]. The color edges that failed all intra-frame demosaicking methods have discontinuities in both luminance and chrominance. For sharp edges of highly saturated colors of weak spectral correlation, no sufficient information exists within a frame to reconstruct the color signal. This is the situation where the temporal correlation can come to the rescue.

Fig. 13(h) and Fig. 14(h) are the results by the temporal demosaicking method in [24]. It offers better visual quality than intra-frame demosaicking, but some color artifacts still exist and the improvement in PSNR is quite small (referring to Table III). Fig. 13(i) and Fig. 14(i) are the demosaicked images by the proposed temporal demosaicking method. The proposed method has clear advantages over all others in terms of visual quality. Most of the color artifacts are eliminated and many sharp edge structures that are missing or distorted in intra-frame demosaicking. The PSNR results (we demosaicked eight consecutive frames and computed the average PSNR) of the three color channels by these demosaicking methods are listed in Table III.

<sup>1</sup>Our thanks to the IMAX Corporation, Mississauga, ON, Canada, for providing the test data.



Fig. 14. Zoom-in images of the demosaicked results. (a) Original image; demosaicked images by the methods in (b) [7]; (c) [4]; (d) [9]; (e) [16]; (f) [15]; (g) [26]; (h) [24]; and (i) the proposed temporal scheme.

Fig. 15. (a) Original image; demosaicked images by the methods in (b) [7]; (c) [4]; (d) [9]; (e) [16]; (f) [15]; (g) [26]; (h) [24]; and (i) the proposed temporal scheme.









(c)





The proposed method achieves significantly higher PSNR than others as well.

The other test sequence, shown in Fig. 12(b), is a skating girl. In this scene, both the object (the girl) and the camera are moving. The motion is a combination of rotation and translation. The video is captured at 24-frames/second and 8 bits per color channel. The original resolution of the sequence is 1948  $\times$  1280 and we down-sampled it to 974  $\times$  640 in the experiment. Fig. 15(a) shows a zoom-in crop (128  $\times$  128) of the scene. As in the previous example, by comparing the other demosaicking techniques in Fig. 15(b)–(h) with the proposed temporal method in Fig. 15(i), we see that most of the color artifacts and zipper effects are suppressed by the proposed method. The PSNR results are also listed in Table III. The proposed method had limited PSNR improvement on the green channel because the green signal of this sequence is so smooth that the spatial demosaicking by itself suffices for good reconstruction.

Finally, we want to bring the reader's attention to the significant PSNR increases in the reconstructed red and blue channels by the proposed demosaicking method. This means that besides reducing color artifacts the proposed method also reproduces the color tones more precisely than other methods. The big improvements in reproduction precision of the red and blue channels should not come as a surprise, considering that the Bayer CFA has much lower sampling frequency and inferior sampling grid pattern for the red and blue channels. The design bias of the Bayer CFA against the red and blue channels in favor of the green channel makes the faithful reproduction of the red and blue signals more difficult if color demosaicking is carried out on a frame-by-frame basis. Temporal demosaicking is capable of much higher tone accuracy in color reproduction.

#### VI. CONCLUSION

We proposed an inter-frame color demosaicking approach that utilizes all three forms of pixel correlations: spatial, spectral, and temporal. The green channel is first reconstructed and it acts as an anchor to help recovering the red and blue channels. In reconstructing each one of the three channels, we first interpolate it using an intra-frame demosaicking method and then temporally enhance it with the help of adjacent frames. The experimental results showed that the proposed approach appreciably improved intra-frame spatial color demosaicking techniques, removing much of the color artifacts of the latter and ensuring higher tone accuracy. Temporal color demosaicking requires a fairly large buffer to hold multiple reference frames, and involves quite extensive computations compared with the intra-frame demosaicking. We can reduce the complexity by invoking the proposed temporal color demosaicking algorithm only when infra-frame demosaicking can not produce good outputs. Only at localities of sharp edges and finely structured textures the CPU-intensive temporal color demosaicking will be activated. In smooth regions of an image, which typically constitute the major portion of a scene, the sampling frequency of the color mosaic is high enough to allow correct color demosaicking solely in the spatial domain.

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