

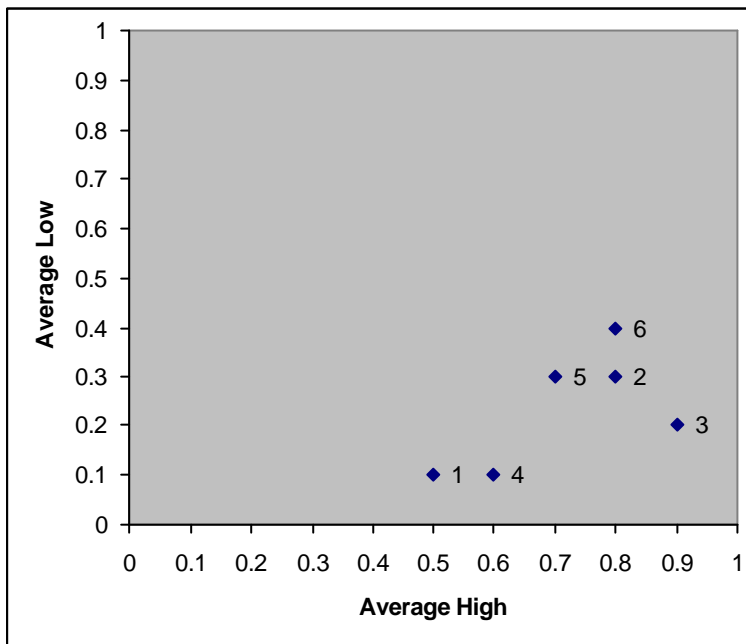
# Supplementary Notes #6

COMP 578 Data Mining and Data Warehousing

MScECT, Semester 1, 03-04

Solutions to exercises in Supplementary Notes #3

1) Using Euclidean distance as the distance metric, the following dissimilarity matrix can be generated



Stock No.	Average High	Average Low
1	0.5	0.1
2	0.8	0.3
3	0.9	0.2
4	0.6	0.1
5	0.7	0.3
6	0.8	0.4

	1	2	3	4	5	6
1	0					
2	0.36	0				
3	0.41	0.14	0			
4	0.1	0.28	0.32	0		
5	0.28	0.1	0.22	0.22	0	
6	0.42	0.1	0.22	0.36	0.14	0

	14	25	3	6
14	0			
25	0.22	0		
3	0.32	0.14	0	
6	0.36	0.1	0.22	0

	14	2	3	5	6
14	0				
2	0.28	0			
3	0.32	0.14	0		
5	0.22	0.1	0.22	0	
6	0.36	0.1	0.22	0.14	0

	14	256
14	0	
2356	0.22	0

—

	14	256	3
14	0		
256	0.22	0	
3	0.32	0.14	0

2)

Let the 2 random initial cluster C1 and C2 be sample 1 and sample 2

$C1 = \{1\}$ ,  $C2 = \{2\}$ ; Center of C1 = {0.5, 0.1}, Center of C2 = {0.8, 0.3}

**Iteration 1:**

- Sample 3  
 $D(3, \text{Center of C1}) = 0.41$ ;  $D(3, \text{Center of C2}) = 0.14$   
 Sample 3 is assigned to C2
- Sample 4  
 $D(4, \text{Center of C1}) = 0.1$ ;  $D(4, \text{Center of C2}) = 0.28$   
 Sample 4 is assigned to C1
- Sample 5  
 $D(5, \text{Center of C1}) = 0.28$ ;  $D(5, \text{Center of C2}) = 0.1$   
 Sample 5 is assigned to C2
- Sample 6  
 $D(6, \text{Center of C1}) = 0.42$ ;  $D(6, \text{Center of C2}) = 0.1$   
 Sample 6 is assigned to C2

$C1 = \{1,4\}$ ,  $C2 = \{2,3,5,6\}$

New centers for C1 = (0.55, 0.1) for C2=(0.8, 0.3)

**Iteration 2:**

- Sample 1  
 $D(1, \text{Center of C1}) = 0.05$ ;  $D(1, \text{Center of C2}) = 0.36$   
 Sample 1 is assigned to C1
- Sample 2

$$D(2, \text{Center of C1}) = 0.32; \quad D(3, \text{Center of C2}) = 0$$

Sample 2 is assigned to C2

- Sample 3

$$D(3, \text{Center of C1}) = 0.36; \quad D(3, \text{Center of C2}) = 0.14$$

Sample 3 is assigned to C2

- Sample 4

$$D(4, \text{Center of C1}) = 0.05; \quad D(4, \text{Center of C2}) = 0.28$$

Sample 4 is assigned to C1

- Sample 5

$$D(5, \text{Center of C1}) = 0.25; \quad D(5, \text{Center of C2}) = 0.1$$

Sample 5 is assigned to C2

- Sample 6

$$D(6, \text{Center of C1}) = 0.39; \quad D(6, \text{Center of C2}) = 0.1$$

Sample 6 is assigned to C2

The centers do not have any changes, the algorithm stops.

3)



From left to right, label them as 1 - 9

Each face has 10 features.

- Addition of 1:  
Assigns 1 to cluster 1 (C1)
- Addition of 2:  
 $S(C1, 2) = S(1, 2) = -2$   
Assigns 2 to cluster 2 (C2)
- Addition of 3:  
 $S(C1, 3) = S(1, 3) = 4$   
 $S(C2, 3) = S(2, 3) = 2$   
Assigns 3 to cluster 1 (C1)
- Addition of 4:  
 $S(C1, 4) = S(1, 4) + S(3, 4) = 2 + -2 = 0$   
 $S(C2, 4) = S(2, 4) = -4$   
Assigns 4 to cluster 2 (C3)
- Addition of 5:  
 $S(C1, 5) = S(1, 5) + S(3, 5) = 2 + 2 = 4$   
 $S(C2, 5) = S(2, 5) = 2$   
 $S(C3, 5) = S(4, 5) = -2$   
Assigns 5 to cluster 2 (C1)
- Addition of 6:  
 $S(C1, 6) = S(1, 6) + S(3, 6) + S(5, 6) = -2 + 2 + 2 = 2$   
 $S(C2, 6) = S(2, 6) = 6$   
 $S(C3, 6) = S(4, 6) = 0$   
Assigns 6 to cluster 2 (C2)

- Addition of 7:

$$S(C1, 7) = S(1, 7) + S(3, 7) + S(5, 7) = -6 + -4 + 0 = -10$$

$$S(C2, 7) = S(2, 7) + S(6, 7) = -2 + -4 = -6$$

$$S(C3, 7) = S(4, 7) = -4$$

Assigns 7 to cluster 4 (C4)

- Addition of 8:

$$S(C1, 8) = S(1, 8) + S(3, 8) + S(5, 8) = 2 + 2 + 4 = 8$$

$$S(C2, 8) = S(2, 8) + S(6, 8) = -2 + -2 = -4$$

$$S(C3, 8) = S(4, 8) = 0$$

$$S(C4, 8) = S(7, 8) = 0$$

Assigns 8 to cluster 1 (C1)

- Addition of 9:





$$S(C1, 9) = S(1, 9) + S(3, 9) + S(5, 9) + S(8, 9) = 0 + -2 + -6 + -4 = -12$$

$$S(C2, 9) = S(2, 9) + S(6, 9) = -8 + -6 = -14$$

$$S(C3, 9) = S(4, 9) = -2$$

$$S(C4, 9) = S(7, 9) = -4$$

Assigns 9 to cluster 5 (C5)

<p>Cluster 1:</p> 	<p>Cluster 4:</p> 
<p>Cluster 2:</p> 	<p>Cluster 5:</p> 
<p>Cluster 3:</p> 