# Supplementary Notes \#5 

COMP 578 Data Mining and Data Warehousing
MScECT, Semester 1, 03-04

## Supplementary Notes \#2 Solution

1) No need to normalize the attribute, because they are of the same type and measured on same scale.

| Customer <br> No. | Normalized <br> Salary | Normalized <br> Age | Approved? <br> Yes/No | Loan Amount <br> ('000) | Normalized <br> Distance with <br> Applicant |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1231 | 0.5 | 0.2 | Y | 12 | 0.32 |
| 1448 | 0.7 | 0.5 | Y | 15 | 0.22 |
| 4567 | 0.9 | 0.7 | N | 23 | 0.41 |
| 7659 | 1.0 | 0.5 | Y | 44 | 0.28 |
| 5355 | 0.8 | 0.4 | N | 37 | 0.1 |
| 8800 | 0.7 | 0.4 | Y | 31 | 0.14 |

The decisions of the 5 nearest neighbors are $\{S, B, B, B, B\}$. Therefore, the decision should be "Buy"

Expected return $=(44+37+31+15+12) / 5=27.8$
2) A linear line can separate two classes. You can find the equation of the line if you wish to.


Let $I L=$ income level, $P M=$ payment method, $F C=$ frequency of call, $\mathrm{LP}=$ any late payment and $\mathrm{CR}=$ credit rating

The sample $X$ we wish to classify, $X=(I L=$ low, $P M=$ cheque, $F C=$ frequent, $L P=$ yes $)$

We need to maximize $P\left(X \mid C_{i}\right) P\left(C_{i}\right)$, for $i=1,2 . P\left(C_{i}\right)$, the prior probability of each class, can be computed based on the training samples:

$$
\begin{aligned}
& P(C R=G o o d)=6 / 10=0.6 \\
& P(C R=B a d)=4 / 10=0.4
\end{aligned}
$$

To compute $P\left(X \mid C_{i}\right)$, for $i=1,2$, we compute the following conditional probabilities:

$$
\begin{aligned}
& \mathrm{P}(I L=\text { low } \mid C R=\mathrm{Good})=1 / 6 \\
& \mathrm{P}(I L=\text { low } \mid C R=\mathrm{Bad})=3 / 4 \\
& \mathrm{P}(\mathrm{PM}=\text { cheque } \mid \mathrm{CR}=\mathrm{Good})=2 / 6 \\
& \mathrm{P}(\mathrm{PM}=\text { cheque } \mid \mathrm{CR}=\mathrm{Bad})=2 / 4 \\
& \mathrm{P}(\mathrm{FC}=\text { frequent } \mid \mathrm{CR}=\mathrm{Good})=2 / 6 \\
& \mathrm{P}(\mathrm{FC}=\text { frequent } \mid \mathrm{CR}=\mathrm{Bad})=3 / 4 \\
& \mathrm{P}(\mathrm{LP}=\text { yes } \mid \mathrm{CR}=\mathrm{Good})=2 / 6 \\
& \mathrm{P}(\mathrm{LP}=\text { yes } \mid \mathrm{CR}=\mathrm{Bad})=3 / 4
\end{aligned}
$$

Using the above probabilities, we obtain:
$P(X \mid C R=$ Good $) P(C R=$ Good $)=\left(\frac{1}{6} \times \frac{2}{6} \times \frac{2}{6} \times \frac{2}{6}\right) \frac{6}{10}=0.0037$
$P(X \mid C R=B a d) P(C R=B a d)=\left(\frac{3}{4} \times \frac{2}{4} \times \frac{3}{4} \times \frac{3}{4}\right) \frac{4}{10}=0.084375$

Therefore the naive Bayesian classifier predicts "CR = Bad" for sample $X$.
4)

$$
\begin{aligned}
M\left(" C R^{\prime \prime}\right) & =\left[-\frac{4}{10} \log _{2} \frac{4}{10}\right]+\left[-\frac{6}{10} \log _{2} \frac{6}{10}\right] \\
& =0.5288+0.4422 \\
& =0.971
\end{aligned}
$$

Consider the splitting according to the "Income level"

|  | Bad | Good | $I(B, G)$ |
| :---: | :---: | :---: | :---: |
| Low | 3 | 1 | 0.811 |
| Medium | 0 | 3 | 0 |
| High | 1 | 2 | 0.918 |

$\{1,2,4,7\}$
$\{5,6,10\}$
$\{3,8,9\}$
B, B, G, B
G, G, G
G, G , B

$$
\begin{aligned}
E\left(" I L^{\prime}\right) & =\frac{4}{10}(0.811)+\frac{3}{10}(0)+\frac{3}{10}(0.918) \\
& =0.3244+0+0.2754 \\
& =0.5998
\end{aligned}
$$

Gain $(" I L ")=0.971-0.5998=0.3712$

Consider the splitting according to the "Payment method"

|  | Bad | Good | I(B,G) |
| :---: | :---: | :---: | :---: |
| Visa | 2 | 2 | 1 |
| Cheque | 2 | 2 | 1 |
| AMEX | 0 | 2 | 0 |

Payment method

$\{1,5,7,8\}$
$\{2,3,6,9\}$
\{4, 10\}
B, G, B, G
B, G, G, B
G, G

$$
\begin{aligned}
E\left(" P M^{\prime}\right) & =\frac{4}{10}(1)+\frac{4}{10}(1)+\frac{2}{10}(0) \\
& =0.4+0.4+0 \\
& =0.8
\end{aligned}
$$

Gain $(" P M ")=0.971-0.8=0.171$

Consider the splitting according to the "Frequency of call"

|  | Bad | Good | I (B,G) |
| :---: | :---: | :---: | :---: |
| Frequent | 3 | 2 | 0.971 |
| Not Frequent | 1 | 4 | 0.722 |


$\{1,2,4,7,10\}$
$\{3,5,6,8,9\}$
$B, B, G, B, G$
G, G, G, G, B

$$
\begin{aligned}
E\left(" F C^{\prime \prime}\right) & =\frac{5}{10}(0.971)+\frac{5}{10}(0.722) \\
& =0.4855+0.361 \\
& =0.8465
\end{aligned}
$$

Gain $\left({ }^{\prime \prime} F C^{\prime \prime}\right)=0.971-0.8465=0.1245$

Consider the splitting according to the "Late payment"
Late payment

|  | Bad | Good | $I(B, G)$ |
| :---: | :---: | :---: | :---: |
| Yes | 3 | 2 | 0.971 |
| No | 1 | 4 | 0.722 |

$$
\begin{aligned}
E\left(" L P^{\prime \prime}\right) & =\frac{5}{10}(0.971)+\frac{5}{10}(0.722) \\
& =0.4855+0.361 \\
& =0.8465
\end{aligned}
$$

Gain $(" L P ")=0.971-0.8465=0.1245$

Among four information gain values, the "Income level" has the largest value.
Therefore, select "Income level" as the root of the decision tree.


Consider the "Low" branch of the root node

$$
\begin{aligned}
M\left(" C R^{\prime}\right) & =\left[-\frac{1}{4} \log _{2} \frac{1}{4}\right]+\left[-\frac{3}{4} \log _{2} \frac{3}{4}\right] \\
& =0.5+0.3113 \\
& =0.8113
\end{aligned}
$$

Consider the splitting according to the "Payment method"

|  | Bad | Good | $I(B, G)$ |
| :---: | :---: | :---: | :---: |
| Visa | 2 | 0 | 0 |
| Cheque | 1 | 0 | 0 |
| AMEX | 0 | 1 | 0 |

$E\left(" P M^{\prime \prime}\right)=\frac{2}{4}(0)+\frac{1}{4}(0)+\frac{1}{4}(0)=0$


Gain $\left(" P M^{\prime \prime}\right)=0.8113-0=0.8113$

Consider the splitting according to the "Frequency of call"

|  | Bad | Good | $\mathrm{I}(\mathrm{B}, \mathrm{G})$ |
| :---: | :---: | :---: | :---: |
| Frequent | 3 | 1 | 0.811 |
| Not Frequent | 0 | 0 | 0 |


$\{1,2,4,7$,
$E\left(" F C^{\prime \prime}\right)=\frac{4}{4}(0.811)+\frac{0}{4}(0)=0.811$
B, B, G, B
$\operatorname{Gain}\left({ }^{\prime \prime} F C^{\prime \prime}\right)=0.811-0.811=0$

Consider the splitting according to the "Late payment"

|  | Bad | Good | $I(B, G)$ |
| :---: | :---: | :---: | :---: |
| Yes | 2 | 1 | 0.918 |
| No | 1 | 0 | 0 |


$\{1,4,7\}$
B, G, B

$$
E\left(" L P^{\prime \prime}\right)=\frac{3}{4}(0.918)+\frac{1}{4}(0)=0.6885
$$

\{2\}
B
$\operatorname{Gain}(" L P ")=0.811-0.6885=0.1225$

Among three information gain values, the "Payment method" has the largest value.
Therefore, select "Payment method" as the node in the "Low" branch.


Consider the remaining entries, the final decision tree should be:


According to the decision tree above, the sample X is predicted as "Bad".

