

Student ID: _____, Last Name , First Name _____

Q1.

10 pts

Q1. Pixel based image processing, read image, display image, intensity adjustment, denoising and edge detection. Please submit your solution electronically. Fill in the required figures and results, as well as matlab code in this document.

[Q1.a: 2pts] Read in the images “lena” and “cameraman”, display the central 100 x 100 pixel portion of images:

Fig. 1a, 100x100 portion of lena

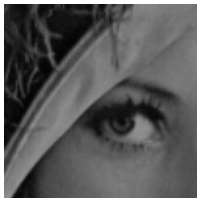


Fig. 1b. 100 x 100 portion of cameraman



Matlab Code:

```
cameraman=imread('cameraman.tif');  
[nRow,nColumn]=size(cameraman);  
cameraman_crop=cameraman(nRow/2-50:nRow/2+49,nColumn/2-50:nColumn/2+49);  
figure(1);  
imshow(cameraman_crop);
```

```
lena=imread('lena.bmp');  
[nRow,nColumn]=size(lena);  
lena_crop=lena(nRow/2-50:nRow/2+49,nColumn/2-50:nColumn/2+49);  
figure(2);  
imshow(lena_crop);
```

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[Q1.b: 8pts] Create noisy images, using `imnoise(im, 'salt&pepper', lv)` from Matlab, using levels 0.01, 0.02, 0.03 and 0.04, (camera man example shown below):



Show de-noising results with Average and Median filters of size 3x3, 5x5 and 11x11. Do not use the `imfilter()`, nor the `medfilter` function from Matlab. Have your own implementation.

Show Matlab code here:

Create Noise

```
cameraman=imread('cameraman.tif');  
[nRow, nColumn]=size(cameraman);  
cameraman1 = imnoise(cameraman, 'salt & pepper',0.01);  
cameraman2 = imnoise(cameraman, 'salt & pepper',0.02);  
cameraman3 = imnoise(cameraman, 'salt & pepper',0.03);  
cameraman4 = imnoise(cameraman, 'salt & pepper',0.04);
```

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Mean Method**3x3**

```
cameraman = imread('cameraman.tif');
[nRow, nColumn]=size(cameraman);
cameraman_noise = imnoise(cameraman,'salt & pepper',0.01);
for i=2:(nRow-1)
for j=2:(nColumn,2)-1)
temp(i, j) = mean(mean(cameraman (i-1:i+1,j-1:j+1)));
end
end
cameraman_denoise = temp;
imshow (cameraman_denoise);
```

5x5

```
cameraman = imread('cameraman.tif');
[nRow, nColumn]=size(cameraman);
cameraman_noise = imnoise(cameraman,'salt & pepper',0.01);
for i=3:(nRow -2)
for j=3:(nColumn-2)
temp(i, j) = mean(mean(cameraman (i-2:i+2,j-2:j+2)));
end
end
cameraman_denoise = temp;
imshow (cameraman_denoise);
```

11x11

```
cameraman = imread('cameraman.tif');
[nRow, nColumn]=size(cameraman);
cameraman_noise = imnoise(cameraman,'salt & pepper',0.01);
for i=6:(nRow-5)
for j=6:(nColumn-5)
temp(i, j) = mean(mean(cameraman (i-5:i+5,j-5:j+5)));
end
end
cameraman_denoise = temp;
imshow (cameraman_denoise);
```

Median Method**3x3**

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```
cameraman = imread('cameraman.tif');
[nRow, nColumn]=size(cameraman);
cameraman_noise = imnoise(cameraman,'salt & pepper',0.01);
for i=2:(nRow-1)
for j=2:(nColumn-1)
temp(i, j) = median(median(cameraman1 (i-1:i+1,j-1:j+1)));
end
end
cameraman_denoise = temp;
imshow (cameraman_denoise);
```

5x5

```
cameraman = imread('cameraman.tif');
[nRow, nColumn]=size(cameraman);
cameraman_noise = imnoise(cameraman,'salt & pepper',0.01);
for i=3:(nRow-2)
for j=3:(nColumn-2)
temp(i, j) = median(median(cameraman1 (i-1:i+1,j-1:j+1)));
end
end
cameraman_denoise = temp;
imshow (cameraman_denoise);
```

11x11





```
cameraman = imread('cameraman.tif');
[nRow, nColumn]=size(cameraman);
cameraman_noise = imnoise(cameraman,'salt & pepper',0.01);
for i=6:(nRow-5)
for j=6:(nColumn-5)
temp(i, j) = median(median(cameraman1 (i-1:i+1,j-1:j+1)));
end
end
cameraman_denoise = temp;
imshow (cameraman_denoise);
```

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Show denoising results here:

Mean

Cameraman Mean (3x3):





Level 0.01	Level 0.02
	
	
Level 0.03	Level 0.04

Cameraman Mean (5x5):

Level 0.01	Level 0.02
	
	
Level 0.03	Level 0.04





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Camerman Mean(11x11):

Level 0.01	Level 0.02
 	 
Level 0.03	Level 0.04





Median

Camerman Median(3x3)





Level 0.01	Level 0.02
 	 
Level 0.03	Level 0.04

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Camerman Median(5x5)

Level 0.01	Level 0.02
	
	
Level 0.03	Level 0.04

Camerman Median(11x11)

Level 0.01	Level 0.02
	
	
Level 0.03	Level 0.04

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Q2.

10 pts

Q2. [10 pts] For the data array given below:

$$x1 = [1.8554 \quad 2.8300 \quad -3.4981 \quad 0.6945 \quad -0.4125 \quad -1.0623 \quad 1.6799 \quad -0.5219];$$

$$x2 = [2.6543 \quad 5.8297 \quad -4.7017 \quad 1.1631 \quad -0.2586 \quad -1.6712 \quad 1.3317 \quad 0.9221];$$

Q2a [3pts] please compute the mean, variance of x1 and x2, show the formula used to compute mean and variance.

$$\text{mean}(X) = \frac{1}{n} \sum_{i=1}^n x_i$$

$$\text{mean}(x1) = 0.1956;$$

$$\text{mean}(x2) = 0.6587;$$

$$\text{Var}(X) = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$$

$$\text{var}(x1) = 4.0368;$$

$$\text{var}(x2) = 9.5003;$$

Q2b [3 pts] compute the covariance between x1 and x2, show the formula also.

$$\text{cov}(X, Y) = E((X - \bar{X})(Y - \bar{Y}))$$

The covariance between x1 and x2 is 5.8978.

Covariance Matrix is defined as:

$$\begin{pmatrix} \text{var}(x_1) & \text{cov}(x_1, x_2) \\ \text{cov}(x_2, x_1) & \text{var}(x_2) \end{pmatrix}$$

$$\text{cov}(x1, x2) =$$

$$4.0368 \quad 5.8978$$

$$5.8978 \quad 9.5003$$

The covariance between x1 and x2 is 5.8978.

Q2c [4 pts] Compute the eigen value and eigen vectors of the covariance between x1 and x2.

$$\text{cov}(x1, x2) =$$

$$4.0368 \quad 5.8978$$

$$5.8978 \quad 9.5003$$

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To calculate the eigenvalue and eigenvector of a matrix X , we calculate:

$$\det(X - \lambda I) = 0;$$

$X =$

$$\begin{array}{cc} 4.0368 & 5.8978 \\ 5.8978 & 9.5003 \end{array}$$

And we obtain

$$\lambda_1 = 0.2688; \lambda_2 = 13.2683$$

To obtain the eigenvector, we calculate $Xv = \lambda v$; correspondingly, we obtain two normalized eigenvector $v_1 = [-0.8427, 0.5384]^T$; $v_2 = [0.5384, 0.8427]^T$

Therefore,

eig_vector =

$$\begin{array}{cc} -0.8427 & 0.5384 \\ 0.5384 & 0.8427 \end{array}$$