# Supplementary Material for Virtual Fully-Connected Layer

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#### 1. Summary

The Supplementary Material will include:

1) The analysis of the corresponding anchor generation methods in Section 2. One is the estimation with a two-layer Multi-layer Perceptron (MLP) based on the attention mechanism. The other one set the  $\{\alpha_{i,l}\}$  to be a constant value and make *anchor*<sub>corr,l</sub> be the centroid.

2) Report the performance on CALFW [9], CPLFW [8], SLLFW [1], and YTF [6] datasets in Section 3. Besides, the TopK accuracy and TAR under varying FAR on IJB-A [3], IJB-B [5], IJB-C [4] datasets are reported on this section.

3) Table 4 in the submitted paper did not report the performance on MegaFace [2] because of the paper width limitation. We report it in Section 4 of this material.

## 2. Analysis of the Corresponding Anchor Generation methods

We propose the corresponding anchor estimated by a weighted average function, as Equation 2 in the submitted paper shows. We copy the equation in the following:

$$anchor_{corr,l} = \frac{\sum_{i=1}^{K} \alpha_{i,l} f_{i,l}}{\sum_{i}^{K} \alpha_{i,l}}$$
(1)

 $f_{i,l}$  is the feature of *i*-th image which belongs to the group *l*. Because we hypothesize there is no anchor conflict in this section, the  $\{f_{i,l}\}(i = 1, 2, ..., K)$  belongs to a single identity.  $\alpha_{i,l}$  is the attention estimation to weight the  $f_{i,l}$ .  $\{\alpha_{i,l}\}$  can be estimated by the attention mechanism or set to be a constant value. If  $\{\alpha_{i,l}\}(i = 1, 2, ..., k)$  equal to a constant value, the *anchor*<sub>corr.l</sub> is the centroid of  $\{f_{i,l}\}$ .

In this section, we analyze two methods of the  $\{\alpha_{i,l}\}$  generation: 1) Constant value. 2) Prediction of an attention module. We build the attention module as a two-layer Multi-layer Perceptron (MLP). The structure of MLP is inspired by the MetaCleaner [7] and illustrated in Figure 1. The comparison of their performance is shown in Table 1. Besides, we sample 10,000 images from the training dataset randomly to get the histograms of  $\{\alpha_{i,l}\}$ . The histograms are shown in the Figure 2.



Figure 1. Weight Estimation Function based on Attention mechanism (MetaCleaner). K is the number of sampling images per identity in a mini-batch.



Figure 2. Histogram of  $\{\alpha_{i,l}\}$ 

Table 1 shows that the performance of two corresponding anchor generation methods is comparable in all three backbones. The histograms in Figure 2 proves that the  $\{\alpha_{i,l}\}$  estimated by an attention module tend to be a constant value (0.5). Based on the discovery, we use the centroid directly in our submitted paper. One of the advantages of using the centroid is that the centroid calculation is flexible because it does not require a fixed K.

### 3. Performance on Several Evaluation Dataset

In this section, we report:

1) The performance on CALFW [9], CPLFW [8], SLLFW [1], and YTF [6] datasets in Table 2

2) The TopK accuracy and TAR under varying FAR on

Network	Strategy	LFW	CFP-FF	CFP-FP	IJB-A	IJB-B	IJB-C	MegaFace
CASIA-Net	Average (Centroid)	98.75±0.27	99.07±0.30	93.04±1.84	91.77	90.78	92.21	81.44
	Weighted Average (Attention Mechanism)	98.77±0.75	99.26±0.39	93.19±1.63	92.37	91.82	91.82	82.72
ResNet-50	Average (Centroid)	99.32±0.27	99.73±0.33	95.77±1.11	92.83	93.21	94.53	93.18
	Weighted Average (Attention Mechanism)	98.33±0.60	99.74±0.29	95.66±1.15	92.79	93.46	94.77	93.47
ResNet-101	Average (Centroid)	99.38±0.38	99.61±0.31	95.55±1.42	93.69	94.05	95.30	94.04
	Weighted Average (Attention Mechanism)	98.70±0.95	99.66±0.30	95.91±1.22	93.11	93.85	95.19	93.45

Table 1. Performance Comparison of Corresponding Anchor Generation Methods.

IJB-A, IJB-B, IJB-C datasets in Table 3, Table 4, and Table 5

We can get all the conclusions that are derived in the submitted paper, again: 1) Our Virtual FC surpasses the lower boundary and all other candidate solutions consistently and significantly. It also achieves comparable performance to the upper boundary with 1% computational resource of the FC layer. 2) The superiority of our Virtual FC is more significant in complex neural network structure (e.g., ResNet50 and ResNet101) than in a simple one (CASIA-Net).

Furthermore, we find the superiority of our Virtual FC is more significant in the tough evaluation datasets/protocols (e.g., CALFW, CPLFW, SLLFW) than the simple ones (e.g., YTF).

		Evalutation Dataset				
		CALFW	CPLFW	SLLFW	YTF	
	lower boundary	86.77	73.60	92.97	93.34	
	upper boundary	90.78	77.9	96.57	94.02	
CASIA Net	N-pair	88.50	74.48	94.00	92.84	
CASIA-NU	Multi-similarity	88.08	74.25	94.02	93.00	
	TCP	88.9 0	76.32	94.47	93.50	
	ours:VFC	89.35	76.78	94.48	93.92	
	lower boundary	87.43	75.45	93.52	93.78	
	upper boundary	94.46	85.03	98.72	95.88	
PorNot 50	N-pair	87.32	72.80	92.28	92.62	
Keshel-J0	Multi-similarity	85.4 0	73.60	91.03	92.76	
	TCP	88.05	76.00	93.23	93.92	
	ours:VFC	91.93	79.00	96.23	95.08	
	lower boundary	88.78	76.72	94.00	93.86	
	upper boundary	94.88	86.23	98.97	96.16	
PorNot 101	N-pair	85.27	74.22	90.97	93.02	
Reside 101	Multi-similarity	85.52	73.07	90.33	92.66	
	TCP	91.45	78.33	95.55	95.14	
	ours:VFC	92.27	79.03	96.67	95.32	

Table 2. Performance On CALFW, CPLFW, SLLFW, YTF

## 4. performance of MegaFace on submitted Table 4

IJB-A		$10^{-1}$	$10^{-2}$	$10^{-3}$	$10^{-4}$
	lower boundary	96.82	89.90	77.61	67.61
	upper boundary	98.04	93.89	83.71	66.17
CASIA-Net	N-pair	95.47	85.65	54.54	17.04
CHOINFILL	Multi-similarity	96.33	85.53	47.18	13.50
	TCP	97.35	89.75	72.22	46.35
	ours:VFC	97.69	91.77	79.41	61.65
	lower boundary	97.11	90.59	78.13	61.53
	upper boundary	98.89	97.33	94.57	90.65
PecNet 50	N-pair	95.95	85.32	70.30	55.03
Resiver-50	Multi-similarity	96.36	83.49	62.81	47.3
	TCP	96.97	85.53	62.71	37.43
	ours:VFC	97.84	92.83	78.72	64.43
	lower boundary	97.24	90.33	78.38	64.05
	upper boundary	99.00	97.81	95.95	93.29
PosNot 101	N-pair	96.72	83.55	62.32	48.06
Kesivel-101	Multi-similarity	95.92	82.02	57.53	36.84
	TCP	97.77	89.23	66.23	40.76
	ours:VFC	98.35	93.69	84.33	73.37

IJB-B		1 vs 1				1 vs N		
		$10^{-1}$	$10^{-2}$	$10^{-3}$	$10^{-4}$	top 1	top 5	top 10
CASIA-Net	lower boundary	96.61	88.40	76.98	55.41	82.3	88.7	90.86
	upper boundary	98.21	93.54	84.25	59.95	85.16	90.45	92.50
	N-pair	97.00	87.25	62.48	15.02	76.71	81.84	83.69
	Multi-similarity	96.95	85.21	55.14	9.33	74.19	80.19	82.96
	TCP	97.41	90.32	76.67	42.5	82.85	88.32	90.41
	ours:VFC	97.68	90.78	78.47	56.55	83.80	89.88	91.77
	lower boundary	97.43	91.26	80.75	59.17	83.91	90.40	92.32
	upper boundary	98.78	96.71	92.16	82.41	90.49	94.04	95.32
PorNot 50	N-pair	97.24	88.46	73.93	55.46	78.01	85.57	88.20
Kesivet-30	Multi-similarity	97.47	88.30	72.32	52.94	75.65	84.53	87.75
	TCP	97.95	90.35	68.17	36.71	82.55	89.51	91.83
	ours:VFC	98.29	93.21	80.92	64.78	86.79	91.95	93.95
	lower boundary	97.32	91.19	80.7	65.56	85.51	91.26	92.97
ResNet-101	upper boundary	98.82	97.01	93.22	83.74	91.91	95.03	96.10
	N-pair	97.47	86.57	69.05	43.65	77.44	86.75	89.57
	Multi-similarity	96.56	85.65	60.50	32.79	79.37	87.51	89.89
	TCP	98.44	92.67	74.52	46.68	86.06	92.57	94.22
	ours:VFC	98.57	94.05	83.26	67.44	86.94	92.82	94.52
	Table 4	Perfc	ormanc	e On l	UB-B			

IJB-C		1 vs 1				1 vs N		
		$10^{-1}$	$10^{-2}$	$10^{-3}$	$10^{-4}$	top 1	top 5	top 10
	lower boundary	97.07	89.94	79.13	56.74	83.64	88.72	90.65
	upper boundary	98.41	94.37	85.59	64.03	86.05	90.4	91.94
CASIA Net	N-pair	97.19	88.69	64.42	14.62	76.71	81.84	83.69
CASIA-NCI	Multi-similarity	97.11	85.90	53.06	10.01	74.29	79.72	81.48
	TCP	97.75	91.86	79.15	48.61	83.53	88.21	89.87
	ours:VFC	97.79	92.21	80.51	60.69	84.58	89.66	91.37
	lower boundary	97.89	92.78	83.4	65.19	84.66	90.20	92.33
	upper boundary	98.94	97.19	93.25	83.94	91.43	94.07	94.98
PosNot 50	N-pair	97.44	90.08	77.54	61.75	83.60	88.87	90.85
Keshet-30	Multi-similarity	97.73	90.06	75.97	57.82	75.74	83.39	86.32
	TCP	98.16	92.08	74.86	43.58	83.03	89.02	90.91
	ours:VFC	98.48	94.53	84.81	70.12	87.38	91.7	93.39
	lower boundary	97.75	92.38	83.79	71.02	86.51	91.31	92.90
ResNet-101	upper boundary	98.98	97.61	94.25	85.60	92.90	95.02	95.80
	N-pair	97.75	88.72	74.71	51.13	77.75	86.10	88.85
	Multi-similarity	97.09	87.50	65.95	38.87	80.27	87.53	89.83
	TCP	98.76	94.22	79.66	52.71	86.87	91.92	93.72
	ours:VFC	98.84	95.30	86.44	71.47	87.84	92.3	94.27

Table 5. Performance On IJB-C

Network	Strategy	MegaFace
CASIA Not	Sampling	78.15
CASIA-Net	Re-grouping	81.44
PacNat 50	Sampling	84.12
Keshel-30	Re-grouping	93.18
PacNat 101	Sampling	74.94
Keshet-101	Re-grouping	94.04

Table 6. The MegaFace Performance which is ignored in Table 4 of the submitted paper.

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